# **Supersymmetric Challenges**

Manuel Drees

Bonn University



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- 2 Breaking SUSY

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### 1 <u>Introduction</u>: Finetung Problem

In SM: loop corrections to Higgs boson mass diverge quadratically:



$$\delta m_{\phi,t}^2 = \frac{3f_t^2}{8\pi^2} \Lambda^2 + \mathcal{O}(\Lambda/m_\phi)$$

 $\Lambda$ : cut–off for momentum in loop.

 $m_{\phi}$  Likes to be at *highest* relevant mass scale, e.g.  $M_{\rm GUT} \sim 10^{16}$  GeV,  $M_{\rm Planck} \sim 10^{18}$  GeV!

If  $m_{\phi,\text{phys.}}^2 = m_{\phi,0}^2 + \delta m_{\phi}^2 = \stackrel{!}{\simeq} (100 \text{ GeV})^2$ : Need to finetune  $m_{\phi,0}^2$  to 1 part in  $10^{30}$ !

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- Standard cosmology has "flatness problem":

 $\Omega_{\rm BBN} - 1 \simeq 10^{-16} \left( \Omega_{\rm now} - 1 \right)$ 

Here:  $\Omega = \rho/\rho_{crit}$ ;  $\Omega = 1$  means flat Universe. Is solved by inflation, which predicts:

- $\Omega_{\rm now} \simeq 1$
- Approximately scale invariant spectrum of density perturbations

Both predictions were confirmed by WMAP!

# Supersymmetry solves finetuning problem

Postulate symmetry between bosons and fermions: boson  $\rightarrow$  fermion, fermion  $\rightarrow$  boson This is called a supersymmetry to distinguish it from the usual (gauge) symmetries.

Requires doubling of particle spectrum: each known particle gets superpartner!

In particular: higgsino  $\tilde{h}$  is superpartner of Higgs boson  $\phi$ .

Quantum corrections:

$$\delta m_{\phi} \stackrel{=}{\underset{\rm SUSY}{=}} \delta m_{\tilde{h}} \propto \ln \frac{\Lambda}{m_{\phi}}$$
 No quadratic divergencies!

Primary virtue of SUSY!

# **Secondary Virtues of Supersymmetry**

- Biggest possible symmetry of interacting QFT: (Lorentz symmetry) ⊗ (gauge symmetry) ⊗ Supersymmetry !
  HLS theorem
- Local supersymmetry invariance implies invariance under coordinate trafos, i.e. GR: local SUSY  $\equiv$  SUGRA
- New particles *automatically* lead to unification of gauge couplings at scale  $M_{\rm GUT} \simeq 2 \cdot 10^{16}$  GeV.
- Automatically contains good Dark Matter candidate, if R-parity is conserved.

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Two basic approaches:

- Postulate simple form of supersymmetry breaking at some high energy scale: Good for global analyses.
- Allow general values for parameters relevant for specific process: Good for dedicated phenomenological analyses; too many parameters for analysis of all LHC data?

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Works in all models discussed here!



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  - $m_{\widetilde{G}}, m_{\text{moduli}} \sim m_{\widetilde{f}}$  gives cosmological problems

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## Gauge Mediated SUSY Breaking (GMS)

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  - No A-term  $\implies$  smaller  $m_h \implies$  "Little hierarchy problem" worse than in mSUGRA.

K. Choi et al., hep-th/0411066, hep-th/0503216; M. Endo et al., hep-ph/0504036

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- Difficulties: Universality?

## **3** The Little Hierarchy Problem

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Recall: Correction to Higgs mass parameter (in potential)

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• Need  $m_h \ge 114$  GeV,  $m_{H_u}^2 \sim M_Z^2 \Longrightarrow$  few % finetuning inevitable?

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  - "Normal hierarchy" (H. Baer et al., hep-ph/0403214): 3rd generation sfermions heavier than 1st/2nd generation: worse finetuning, but easier DM

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- Simple models still allow rather light sparticles! In mSUGRA:  $m_{\tilde{g}} \geq 360$  to 410 GeV,  $m_{\tilde{\chi}_1^{\pm}} \geq 105$  GeV, ... Djouadi et al., hep-ph/0602001

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- Worry about finetuning only if LHC does not find SUSY!



Is it broken or not?

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- Determine parameters: Need to use all available information: kinematical distributions, (ratios of) cross sections for different final states. For  $m_{\tilde{q},\tilde{g}} \lesssim 1.5$  TeV: no. of observables > no. of parameters!

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- Analyses should be model—independent, or one needs sufficiently many analyses to cover all cases
- Data will quickly narrow down field of candidate models