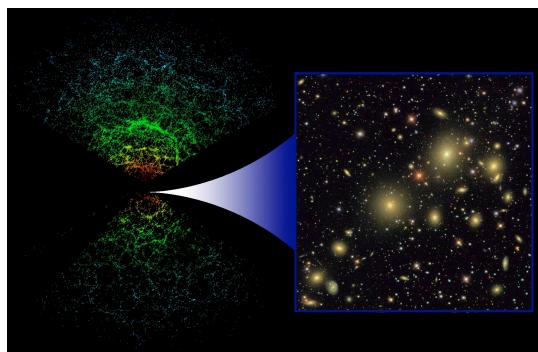


## Sloan Digital Sky Survey (SDSS)



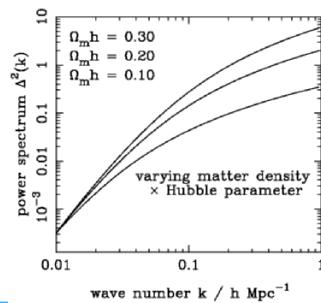
- (SDSS-II) collaboration of over 200 scientists in 14 institutions
- survey measured redshifts for 800,000 galaxies in the local Universe (r-band selection)
- also observed ~100,000 luminous red galaxies out to higher redshift
- all data now taken and publically released: DR7 now available



## Talk outline: Cosmological Physics from 2-pt statistics

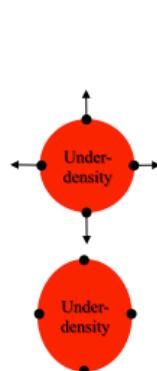
Comoving power spectrum or correlation function

- Matter, baryon densities
- Neutrino mass
- Inflation fluctuation spectrum
- $f_{NL}$



Information from geometry: we measure angles, redshifts

- Galaxy clustering as a standard ruler
- Baryon Acoustic Oscillations
- Alcock-Paczynski effect



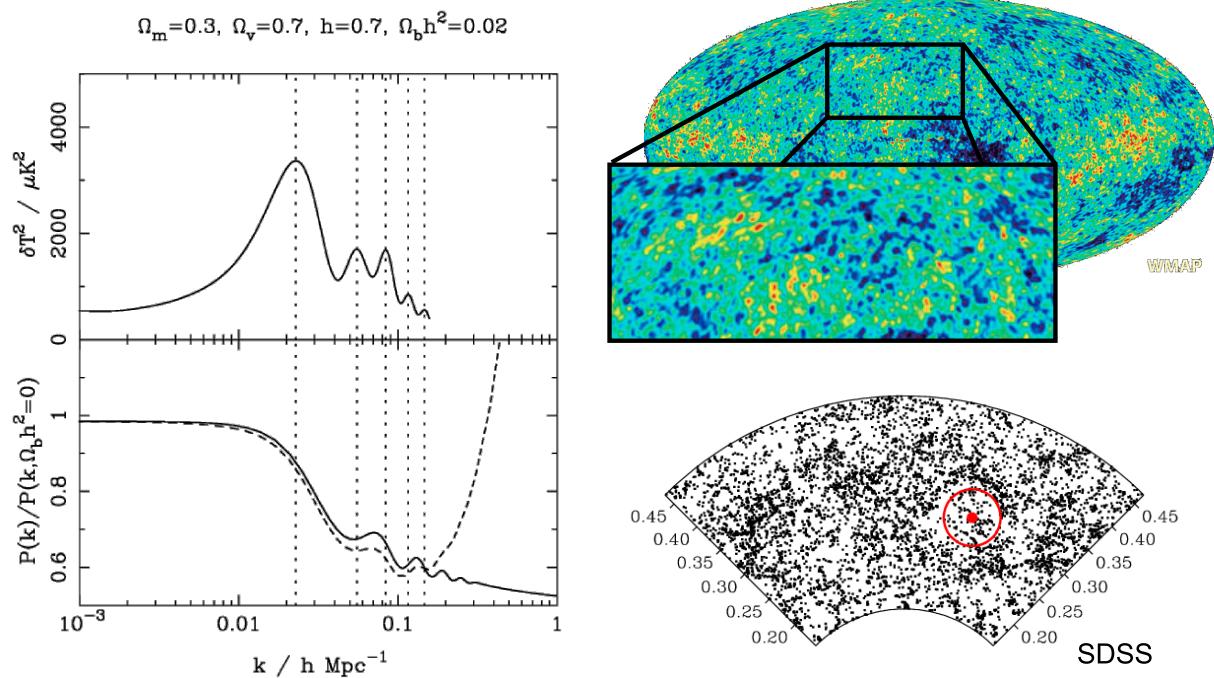
Information from structure growth

- redshift-space distortions
- amplitude of power spectrum

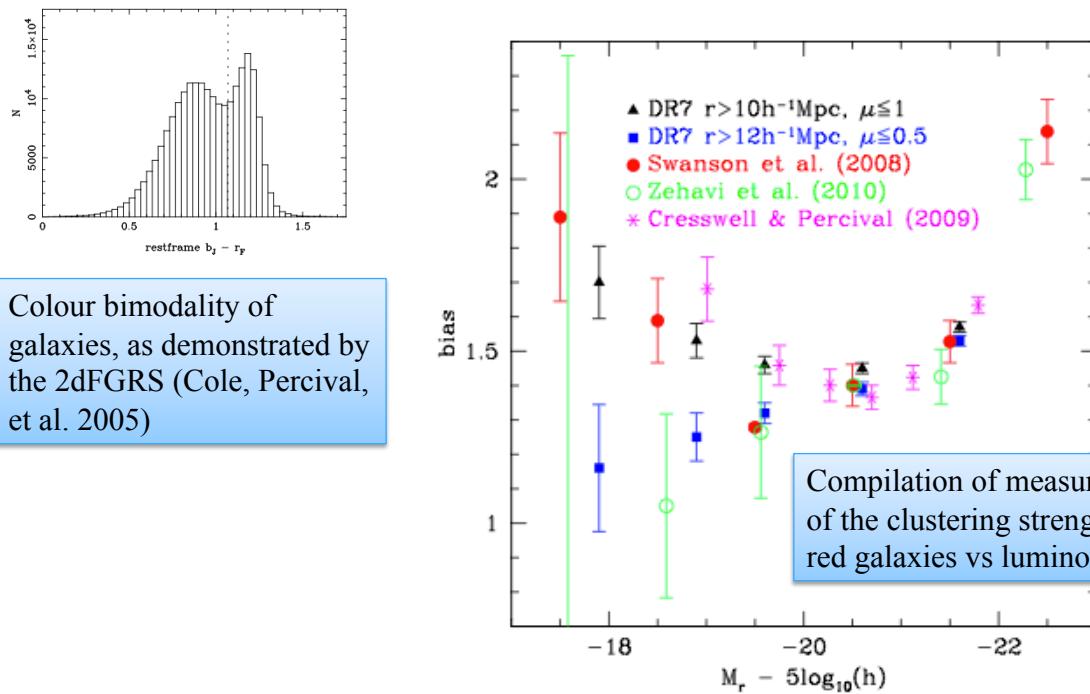
Selected future surveys

Information from the comoving  
power spectrum

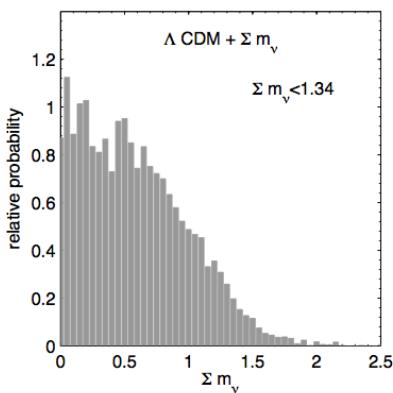
## Relationship between CMB and LSS clustering



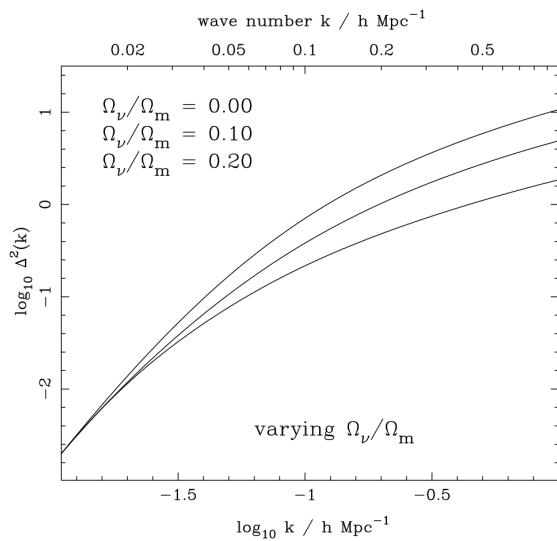
## Problem: we do not observe the mass



## neutrino mass

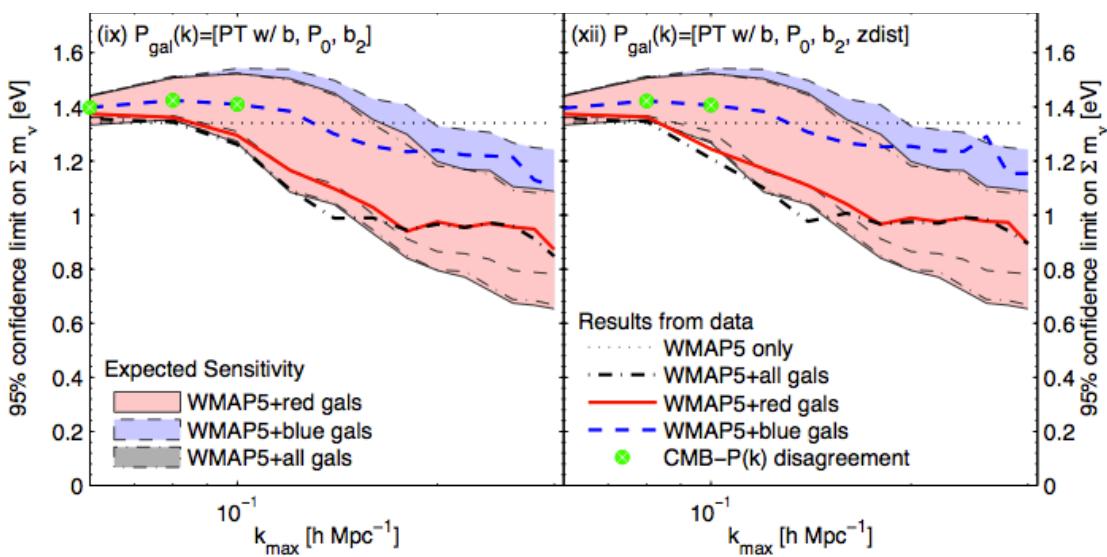


WMAP 7 year data:  
Dunkley et al. (2009: ApJS, 180, 306)



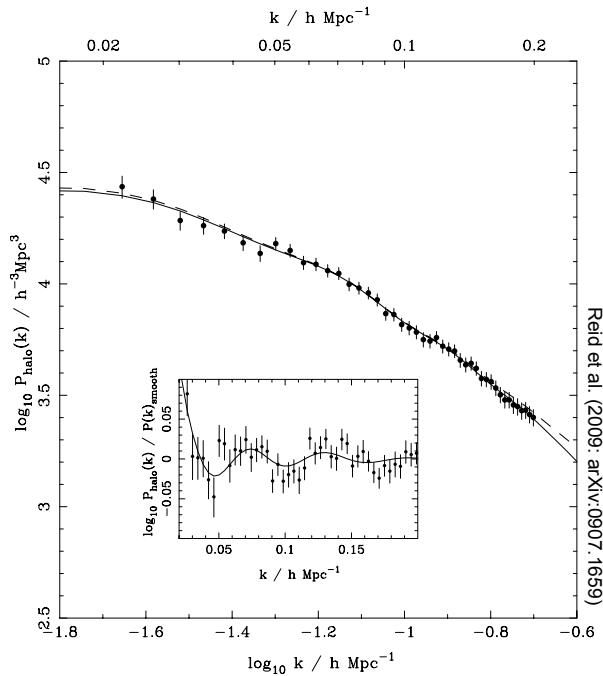
LSS can help through comoving shape  
and breaking CMB projection degeneracies

## neutrino mass



For current SDSS data: red and blue galaxies give  
constraints that are ~1 σ apart, using shape of P(k)

## P(k) fit for SDSS DR7 LRGs



Use luminous red galaxies (LRGs) to extract the halo power spectrum and use the shape to constrain cosmological models

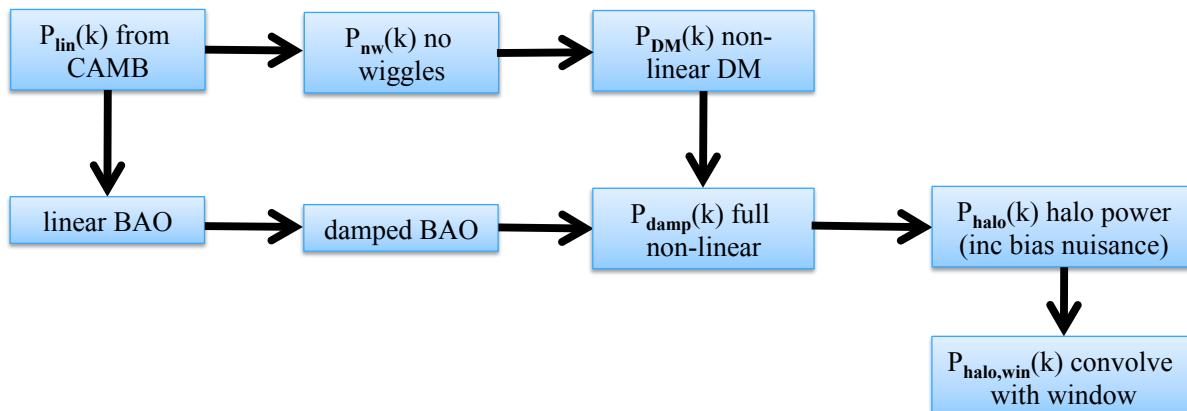
Include information from both shape of P(k) and geometry

Reid, Percival, Eisenstein, et al. (2009, arXiv:0907.1659)

## Have to carefully model non-linearities, bias



$P(k)$	Definition	Reference
$\hat{P}_{LRG}(k)$	measured angle averaged redshift-space power spectrum of the LRGs	-
$\hat{P}_{halo}(k)$	measured power spectrum of reconstructed halo density field	-
$P_{lin}(k)$	linear power spectrum computed by CAMB	Lewis et al. (2000)
$P_{DM}(k)$	theoretical real-space non-linear power spectrum of dark matter	-
$P_{nw}(k)$	theoretical linear power spectrum without BAO ("no wiggles")	Eisenstein & Hu (1998)
$P_{damp}(k)$	theoretical linear power spectrum with damped BAO (Eqn. 10)	Eisenstein et al. (2007b)
$P_{halo}(k, \mathbf{p})$	model for the reconstructed halo power spectrum for cosmological parameters $\mathbf{p}$	Reid et al. (2008)
$P_{halo,win}(k, \mathbf{p})$	$P_{halo}(k, \mathbf{p})$ convolved with survey window function (Eqn. 5) and directly compared with $\hat{P}_{halo}(k)$ in the likelihood calculation (Eqn. 6)	Percival et al. (2007)



Reid, Percival, Eisenstein, et al. (2009, arXiv:0907.1659)

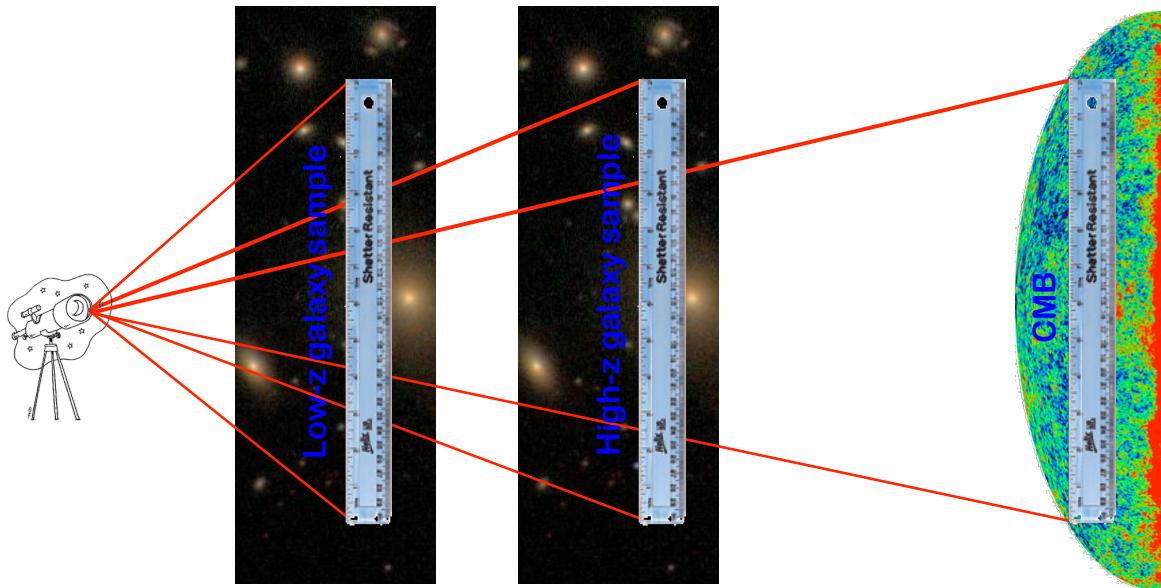


parameter	$\Lambda$ CDM	$\Lambda$ CDM	wCDM	owCDM	owCDM+SN
$\Omega_m$	$0.289 \pm 0.019$	$0.309 \pm 0.025$	$0.328 \pm 0.037$	$0.306 \pm 0.050$	$0.312 \pm 0.022$
$H_0$	$69.4 \pm 1.6$	$66.0 \pm 2.7$	$64.3 \pm 4.1$	$66.7^{+5.9}_{-5.6}$	$65.6 \pm 2.5$
$D_V(0.35)$	$1349 \pm 23$	$1415 \pm 49$	$1398 \pm 45$	$1424 \pm 49$	$1418 \pm 49$
$r_s/D_V(0.35)$	$0.1125 \pm 0.0023$	$0.1084 \pm 0.0034$	$0.1094 \pm 0.0032$	$0.1078^{+0.0033}_{-0.0034}$	$0.1081 \pm 0.0034$
$\Omega_k$	-	$-0.0114^{+0.0076}_{-0.0077}$	-	$-0.009 \pm 0.012$	$-0.0109 \pm 0.0088$
$w$	-	-	$-0.79 \pm 0.15$	$-1.06 \pm 0.38$	$-0.99 \pm 0.11$
$\Omega_A$	$0.711 \pm 0.019$	$0.703 \pm 0.021$	$0.672 \pm 0.037$	$0.703^{+0.057}_{-0.058}$	$0.699 \pm 0.020$
Age (Gyr)	$13.73 \pm 0.13$	$14.25 \pm 0.37$	$13.87 \pm 0.17$	$14.27 \pm 0.52$	$14.24 \pm 0.40$
$\Omega_{\text{tot}}$	-	$1.0114^{+0.0077}_{-0.0076}$	-	$1.009 \pm 0.012$	$1.0109 \pm 0.0088$
$100\Omega_b h^2$	$2.272 \pm 0.058$	$2.274 \pm 0.059$	$2.293^{+0.062}_{-0.063}$	$2.279^{+0.066}_{-0.065}$	$2.276^{+0.060}_{-0.059}$
$\Omega_c h^2$	$0.1161^{+0.0039}_{-0.0038}$	$0.1110 \pm 0.0052$	$0.1112^{+0.0056}_{-0.0057}$	$0.1103^{+0.0055}_{-0.0054}$	$0.1110^{+0.0051}_{-0.0052}$
$\tau$	$0.084 \pm 0.016$	$0.089 \pm 0.017$	$0.088 \pm 0.017$	$0.088 \pm 0.017$	$0.088 \pm 0.017$
$n_s$	$0.961 \pm 0.013$	$0.962 \pm 0.014$	$0.969 \pm 0.015$	$0.965 \pm 0.016$	$0.964 \pm 0.014$
$\ln(10^{10} A_{05})$	$3.080^{+0.036}_{-0.037}$	$3.068 \pm 0.040$	$3.071^{+0.040}_{-0.039}$	$3.064 \pm 0.041$	$3.068 \pm 0.039$
$\sigma_8$	$0.824 \pm 0.025$	$0.796 \pm 0.032$	$0.735 \pm 0.073$	$0.79 \pm 0.11$	$0.790^{+0.045}_{-0.046}$

**Table 3.** Marginalized one-dimensional constraints (68%) for WMAP5+LRG for flat  $\Lambda$ CDM,  $\Lambda$ CDM with curvature ( $\Lambda$ CDM), flat wCDM (wCDM), wCDM with curvature (owCDM), and wCDM with curvature and including constraints from the Union Supernova sample. Here  $\tau$  is the optical depth to reionization,  $n_s$  is the scalar spectral index, and  $A_{05}$  is the amplitude of curvature perturbations at  $k = 0.05/\text{Mpc}$ ; these parameters are constrained directly by the CMB only.

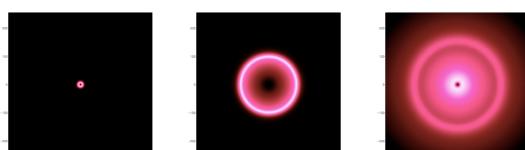
Reid, Percival, Eisenstein, et al. (2009, arXiv:0907.1659)

## Using clustering to measure geometry



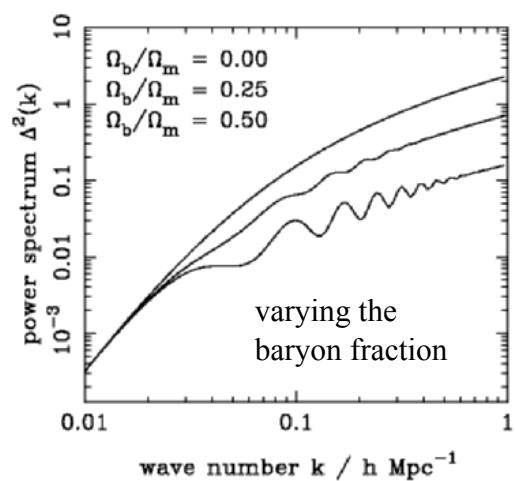
Sunyaev & Zel'dovich (1970); Peebles & Yu (1970); Doroshkevitch, Sunyaev & Zel'dovich (1978); ...  
 Cooray, Hu, Huterer & Joffre (2001); Eisenstein (2003); Seo & Eisenstein (2003);  
 Blake & Glazebrook (2003); Hu & Haiman (2003); ...

## Baryon Acoustic Oscillations (BAO)



(images from Martin White)

To first approximation, BAO wavelength is determined by the comoving sound horizon at recombination



$$k_{\text{bao}} = 2\pi/s$$

$$s = \frac{1}{H_0 \Omega_m^{1/2}} \int_0^{a_*} da \frac{c_s}{(a + a_{\text{eq}})^{1/2}}$$

comoving sound horizon  $\sim 110 h^{-1} \text{Mpc}$ ,  
 BAO wavelength  $0.06 h \text{Mpc}^{-1}$

## BAO measurements

BAO measurements linked to physical BAO scale through:

Radial direction

$$\frac{c}{H(z)} \Delta z$$

Angular direction

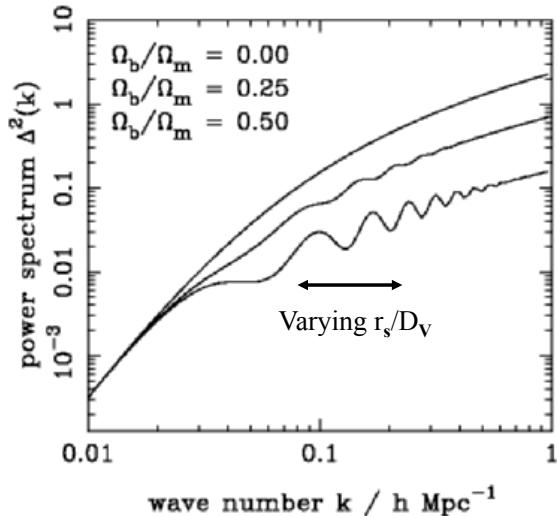
$$(1+z) D_A \Delta \theta$$

To first order, random pairs depend on

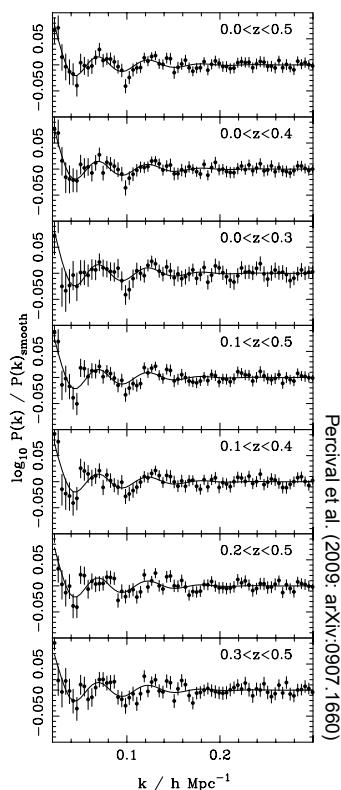
$$D_V(z) = \left[ (1+z)^2 D_A^2(z) \frac{cz}{H(z)} \right]^{1/3}$$

Observed BAO position therefore constrains some multiple of

$$\frac{r_s}{D_V}$$



## BAO in SDSS DR7 + 2dFGRS power spectra



- Combine 2dFGRS, SDSS DR7 LRG and SDSS Main Galaxy samples
- split into redshift slices and fit  $P(k)$  with model comprising smooth fit  $\times$  BAO
- results can be written as independent constraints on a distance measure to  $z=0.275$  and a tilt around this

$r_s(z_d)/D_V(0.275) = 0.1390 \pm 0.0037$  (2.7%)  
 $D_V(0.35)/D_V(0.2) = 1.736 \pm 0.065$

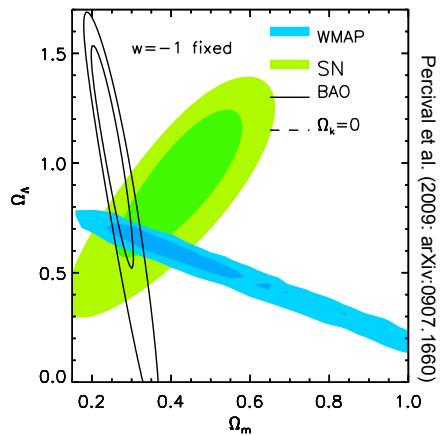
- consistent with  $\Lambda$ CDM models at  $1.1\sigma$  when combined with WMAP5



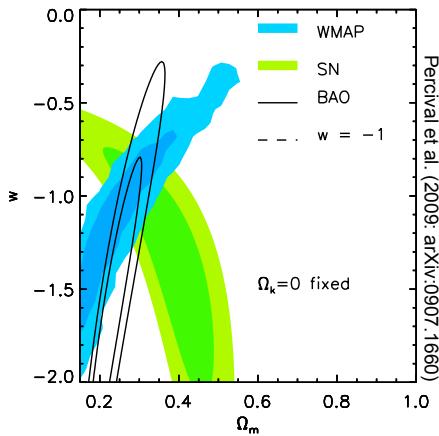
## Comparing BAO constraints vs other data



$\Lambda$ CDM models with curvature



flat wCDM models



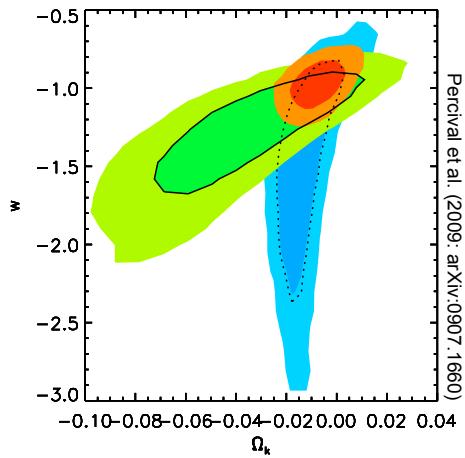
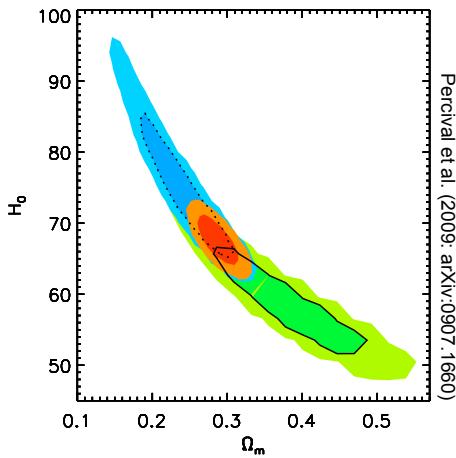
- Union supernovae
- WMAP 5year
- SDSS BAO Constraint on  $r_s(z_d)/D_V(0.2)$  &  $r_s(z_d)/D_V(0.35)$

Percival, Reid, Eisenstein et al. (2009, arXiv:0907.1660)

## BAO + CMB + SN model constraints



w-CDM models with curvature



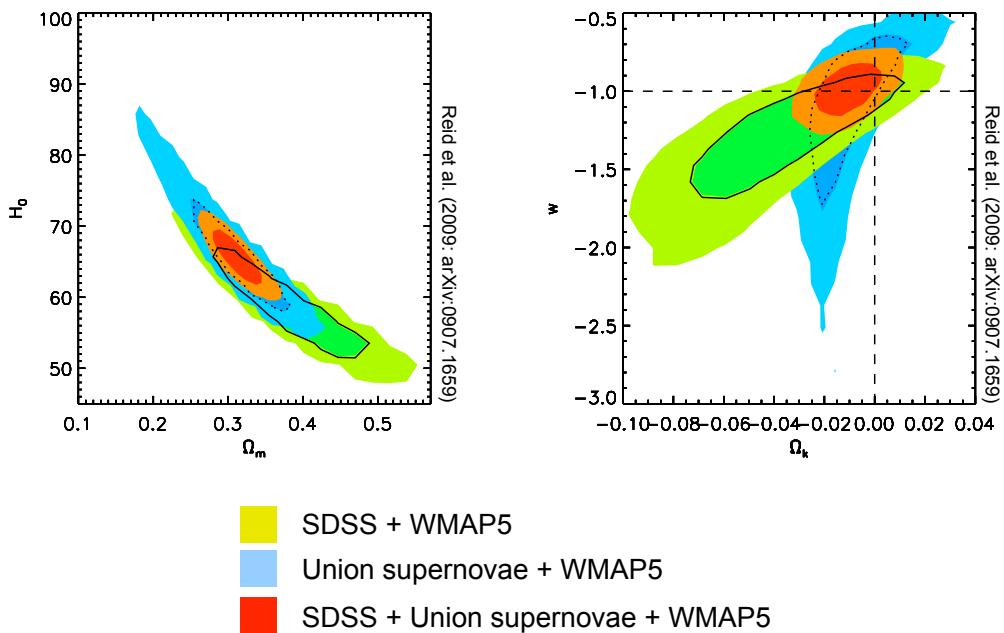
- SDSS + WMAP5
- Union supernovae + WMAP5
- SDSS + Union supernovae + WMAP5

Percival, Reid, Eisenstein et al. (2009, arXiv:0907.1660)

## LRG halo $P(k)$ + CMB + SN model constraints



w-CDM models with curvature



Reid, Percival, Eisenstein, et al. (2009, arXiv:0907.1659)

## Cosmology from redshift-space distortions

## redshift-space distortions

When we measure the position of a galaxy, we measure its position in redshift-space; this differs from the real-space because of its peculiar velocity:

$$s(r) = r - v_r(r)\hat{r}$$

Where  $s$  and  $r$  are positions in redshift- and real-space and  $v_r$  is the peculiar velocity in the radial direction

## RSD on small scales

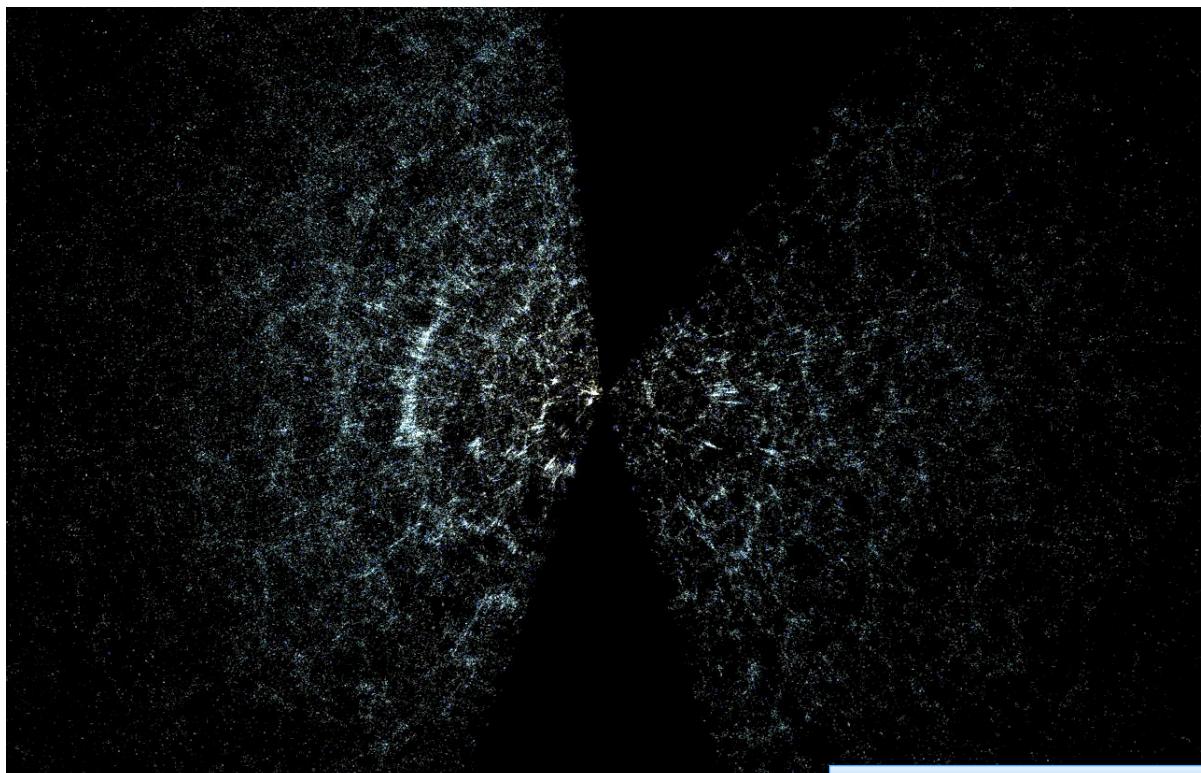
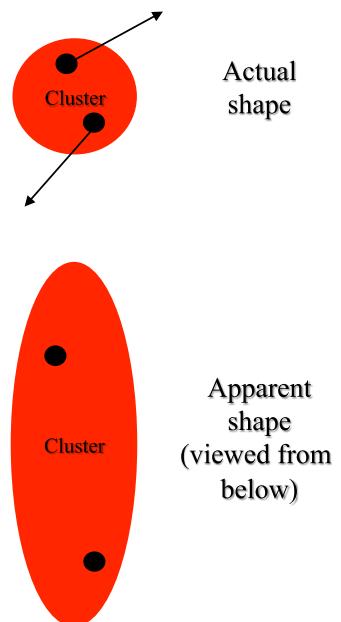


Image of SDSS, from U. Chicago

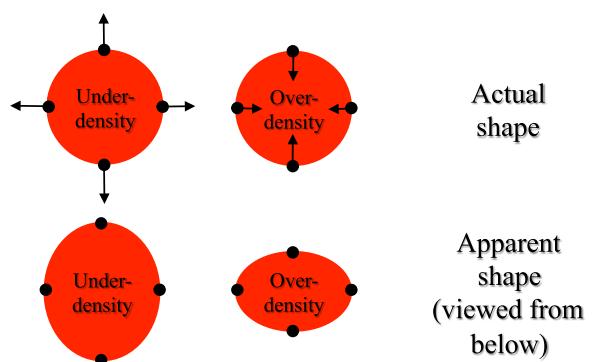
## RSD on small scales

- Virial motions of galaxies in collapsed objects misinterpreted as Hubble flow
- Leads to apparent elongation of clusters along line-of-sight
- non-linear physics, so hard to extract cosmological information



## RSD on large scales

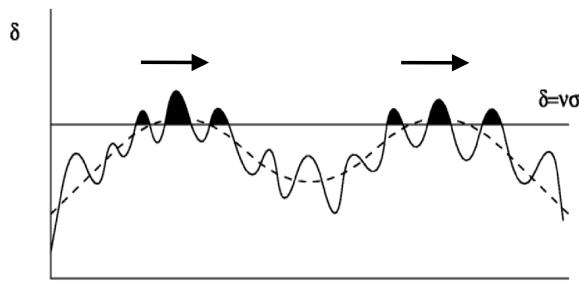
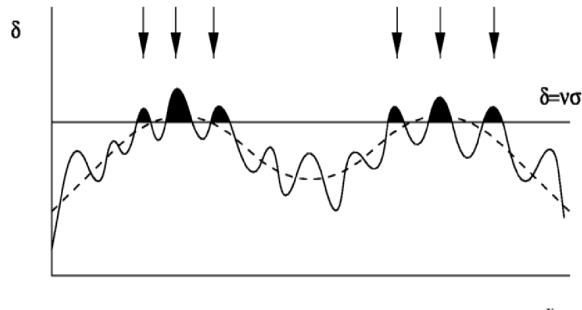
- Structure growth is
  - driven by the motion of matter
  - inhibited by the cosmological expansion
- Motion of galaxies carries an imprint of the rate of growth of large-scale structure.
- On large scales, galaxies move coherently towards the overdensities and away from underdensities



## Galaxies act as test particles

Galaxies act as test particles with the flow of matter

On large-scales, the distribution of galaxy velocities is unbiased provided that the positions of galaxies fully sample the velocity field



Peak velocity bias?

Peak overdensity bias

If fact, we can expect a small peak velocity-bias due to motion in Gaussian random fields

Percival & Schaefer, 2008, MNRAS 385, L78

## What parameter do RSD measure?

Two ways of writing the over-density in linear limit

$$\begin{aligned}\delta_{\text{gal}}(k, \mu) &= b\delta_{\text{mass}}(1 + \mu^2\beta) \\ \delta_{\text{gal}}(k, \mu) &= b\delta_{\text{mass}} + \mu^2 b_v f \delta_{\text{mass}}\end{aligned}$$

Two ways of writing the power spectrum

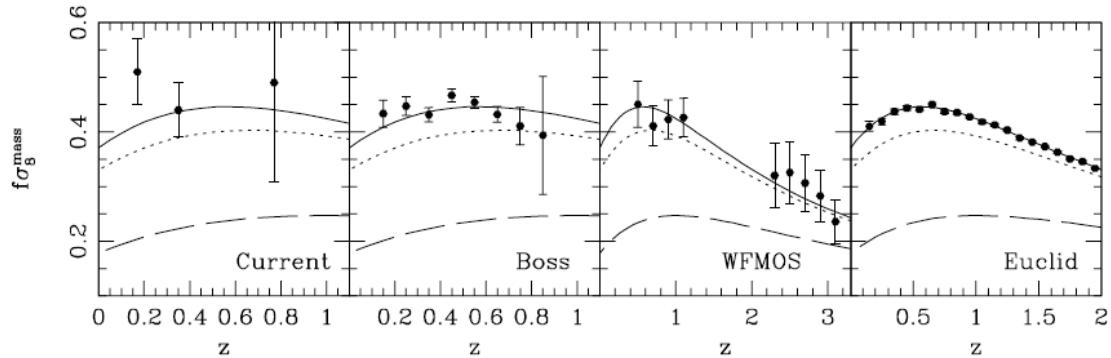
$$\begin{aligned}P_{\text{gal}}(k, \mu) &= b^2 P_{\text{mass}}(1 + \beta\mu^2)^2 \\ P_{\text{gal}}(k, \mu) &= P_{\text{mass}}(b^2 + 2\mu^2 b b_v f + \mu^4 b_v^2 f^2)\end{aligned}$$

We measure the normalizations of the galaxy over-density field ( $b_\delta \sigma_8$ ), and the galaxy velocity field ( $f b_v \sigma_8$ , with  $b_v = 1$ ). You can obviously measure any combinations of these (e.g.  $\beta$ ), or other combinations.

## Do we need to know galaxy bias?

Assuming we know  $b_v$ , RSD constrain  $f\sigma_8$ , the amplitude of the matter velocity power spectrum, which can be as good a test of GR as  $f$ .

$$f \equiv \frac{d \log D}{d \log a} \quad f\sigma_8 \propto \frac{dD}{d \log a}$$



Song, Percival, 2008, astro-ph/0807.0810

## Direct estimator for the velocity power spectrum

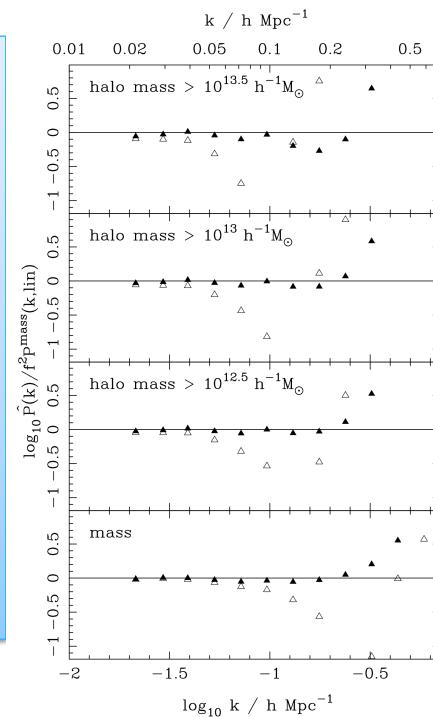
Can construct an estimator for the linear mass velocity power spectrum (mass power spectrum multiplied by  $f^2$ )

$$\hat{P}(k) = \frac{7}{48} \left[ 5(7P_0 + P_2) - \sqrt{35}(35P_0^2 + 10P_0P_2 - 7P_2^2)^{1/2} \right]$$

Where  $P_0$  and  $P_2$  are the standard expansions of the power in Legendre polynomials

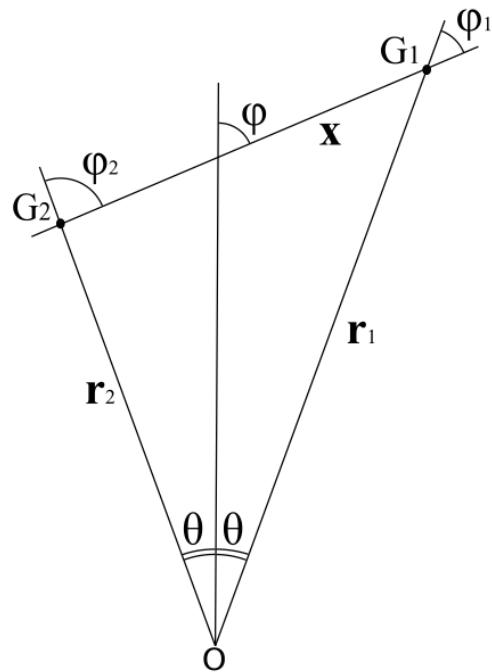
On large-scales, the primary systematic is a possible velocity-bias.

This estimator follows the plane-parallel, distant observer limit



Percival, White, 2008, astro-ph/0808.0003

- Geometry is actually a different triangle for each pair of galaxies
- In plane-parallel limit,
  - $\theta=0$
  - $\phi_1=\phi_2=\phi_3$
  - $\mathbf{r}_1=\mathbf{r}_2$



Raccanelli, Samushai &amp; Percival 2010, arXiv:1006:1652

Following Papai & Szapudi (2008) we can write the full power spectrum

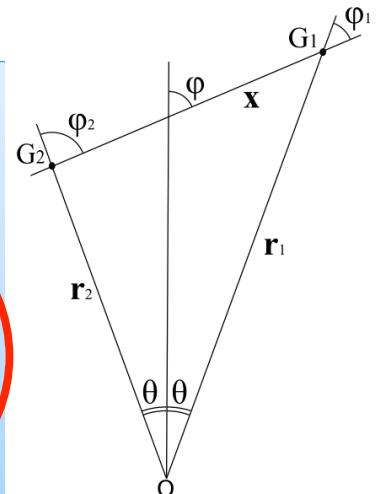
$$\langle \delta^s(\mathbf{r}_1) \delta^{s*}(\mathbf{r}_2) \rangle = \int \frac{d^3 k}{(2\pi)^3} P(k) e^{ik(r_1 - r_2)} \left[ 1 + \frac{f}{3} + \frac{2f}{3} L_2(\mu_1) - \frac{i\alpha f}{r_1 k} L_1(\mu_1) \right] \left[ 1 + \frac{f}{3} + \frac{2f}{3} L_2(\mu_2) - \frac{i\alpha f}{r_2 k} L_1(\mu_2) \right]$$

where

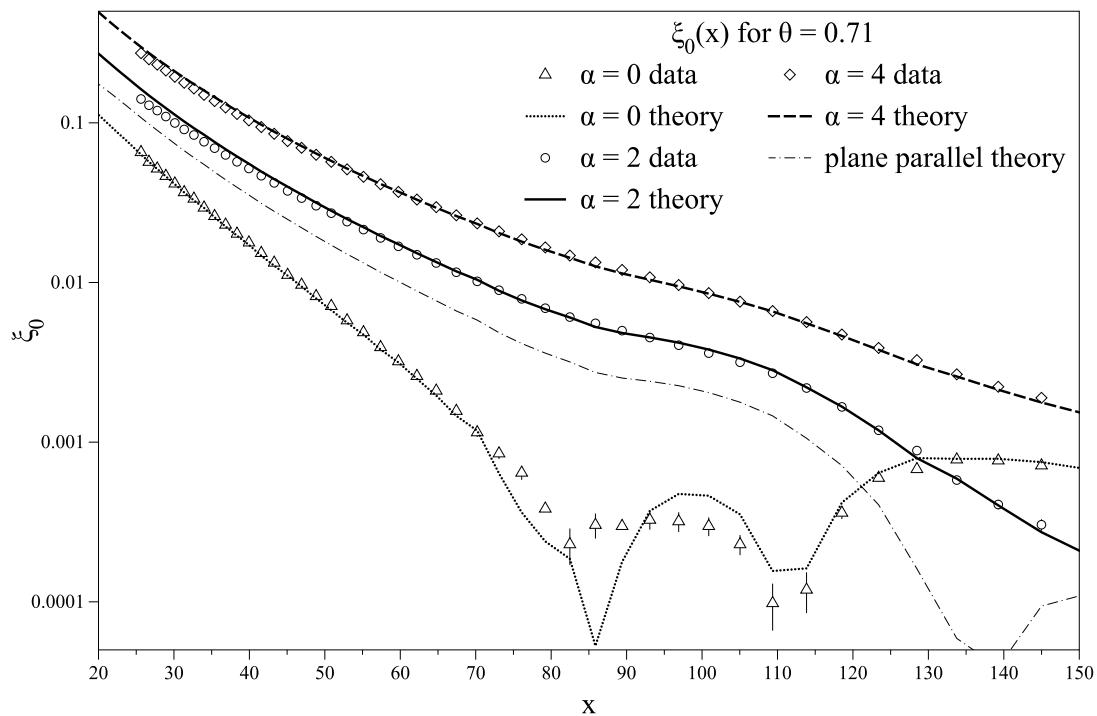
$$\mu_1 = \cos(\phi_1), \quad \mu_2 = \cos(\phi_2)$$

Wide-angle RSD terms

Mode-coupling RSD terms

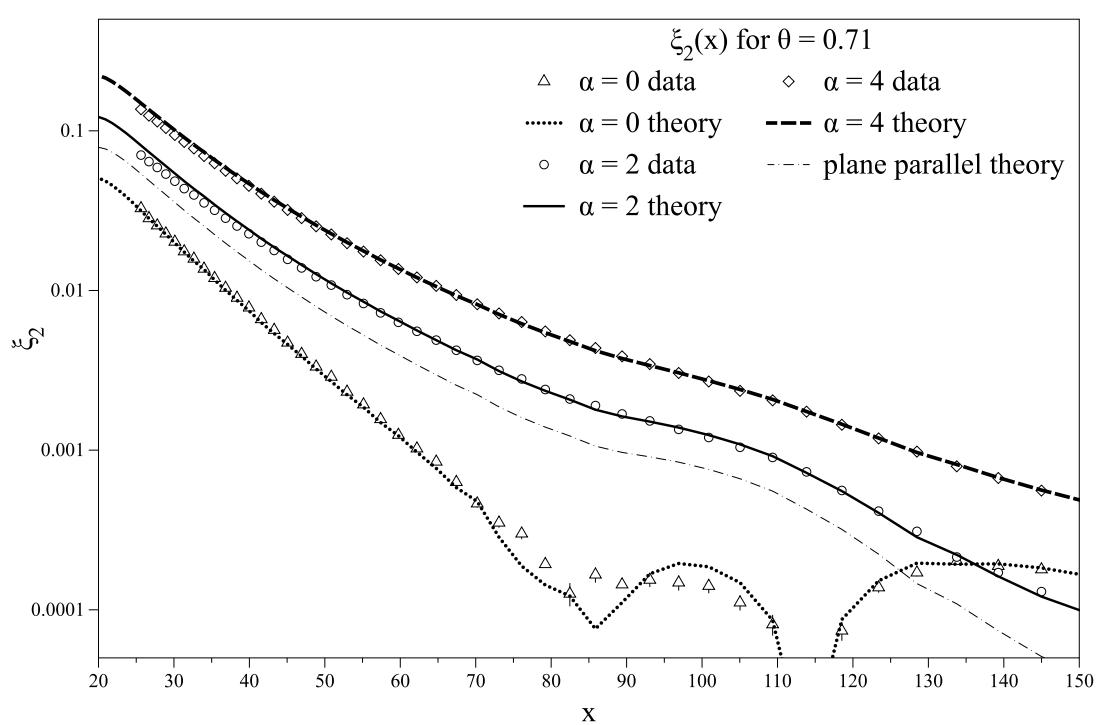


## Testing wide angle RSD: results



Raccanelli, Samushai & Percival 2010, arXiv:1006:1652

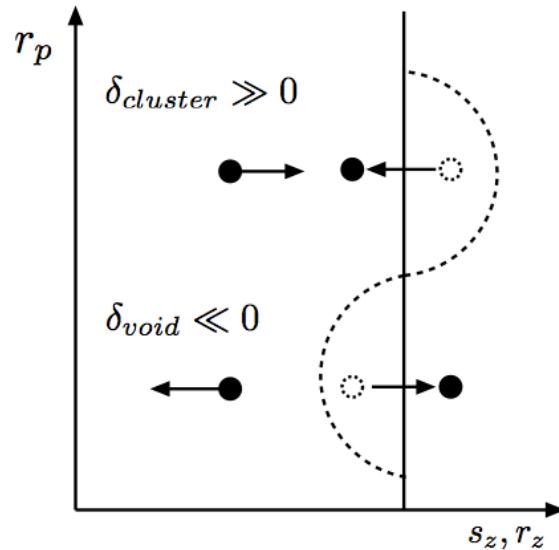
## Testing wide angle RSD: results



Raccanelli, Samushai & Percival 2010, arXiv:1006:1652

## Projected clustering measurements

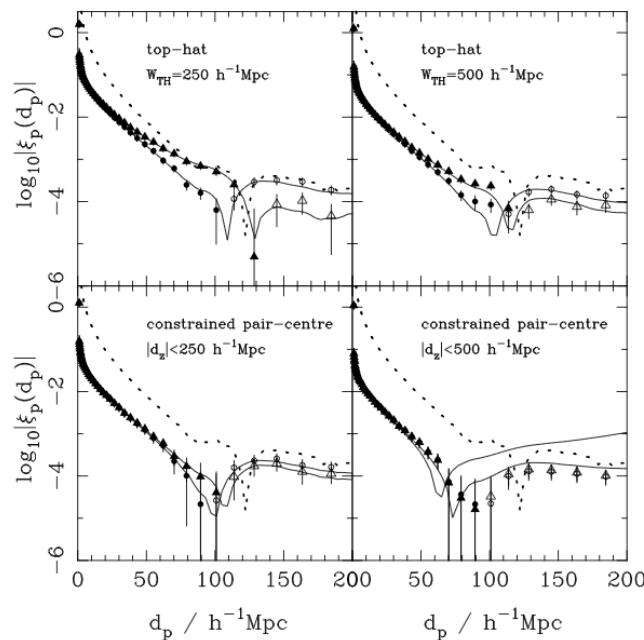
We even have to include RSD when modeling projected measurements (even though RSD do not change angular positions)



Nock, Percival & Ross 2010, arXiv:1003.0896

## Projected clustering measurements

Although there are ways to mitigate RSD effects – for example by binning based on pair centers, rather than galaxy redshifts

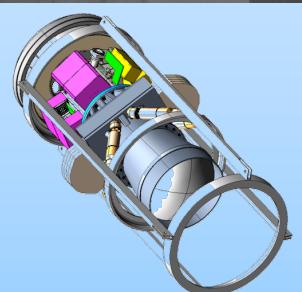
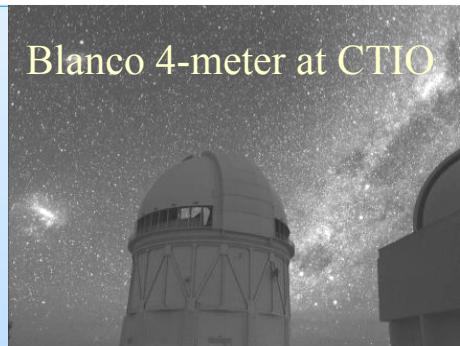


Nock, Percival & Ross 2010, arXiv:1003.0896

## Selected future surveys

## DES: summary

- Survey due to start autumn 2011
- $5000\text{deg}^2$  multi-colour imaging
- Will include IR data from VISTA hemisphere survey
- photo-z for 300,000,000 galaxies
- Will be used to constrain dark energy using 4 probes
  - LSS/BAO
  - weak lensing
  - supernovae
  - cluster number density
- Radial information from photometric redshifts
  - no redshift-space distortions
  - weaker constraints
- See also: Pan-STARRS, VST-VISTA, SkyMapper



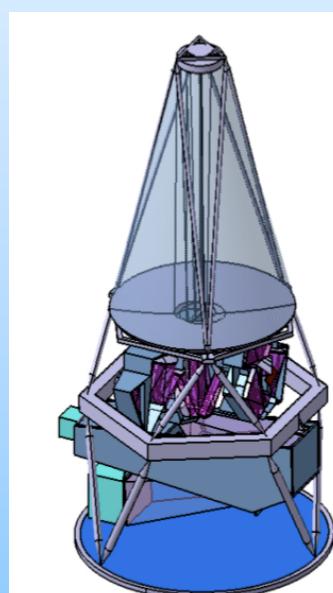
## BOSS: summary

- $\Omega = 10,000 \text{deg}^2$
- Selected from  $11,000 \text{deg}^2$  of imaging
  - $8,500 \text{deg}^2$  in North
  - $2,500 \text{deg}^2$  in South (fill in SDSS-II Southern stripes)
- LRGs :  $150/\text{deg}^2$ ,  $z \sim 0.1 - 0.7$  (direct BAO)
- $1\% d_A$ ,  $1.8\% H$  at  $z \sim 0.35, 0.6$
- QSOs :  $20/\text{deg}^2$ ,  $z \sim 2.1 - 3.0$  (BAO from Ly- $\alpha$  forest)
- $1.5\% d_A$ ,  $1.2\% H$  at  $z \sim 2.5$
- Cosmic variance limited to  $z \sim 0.6$  : as good as LSS mapping will get with a single ground based telescope
- Leverage existing SDSS hardware & software where possible
- Sufficient funding is in place and project is underway
- [www.sdss3.org/boss](http://www.sdss3.org/boss)
- See also: WiggleZ, VIPERS



## Euclid: summary

- ESA Cosmic Vision proposal (600M€, M-class mission)
- Now entering definition phase
- 5 year mission, L2 orbit, 1.2m primary mirror
- nominal 2016 launch date
- $20,000 \text{deg}^2$  imaging and spectroscopic survey
- weak lensing (WL) from imaging survey
- BAO and  $P(k)$  from spectroscopic survey
- combination of probes (BAO, WL, z-space distortions) allows tests of
  - geometry
  - structure formation
- allows fundamental tests of GR
- See also: LSST, BigBOSS



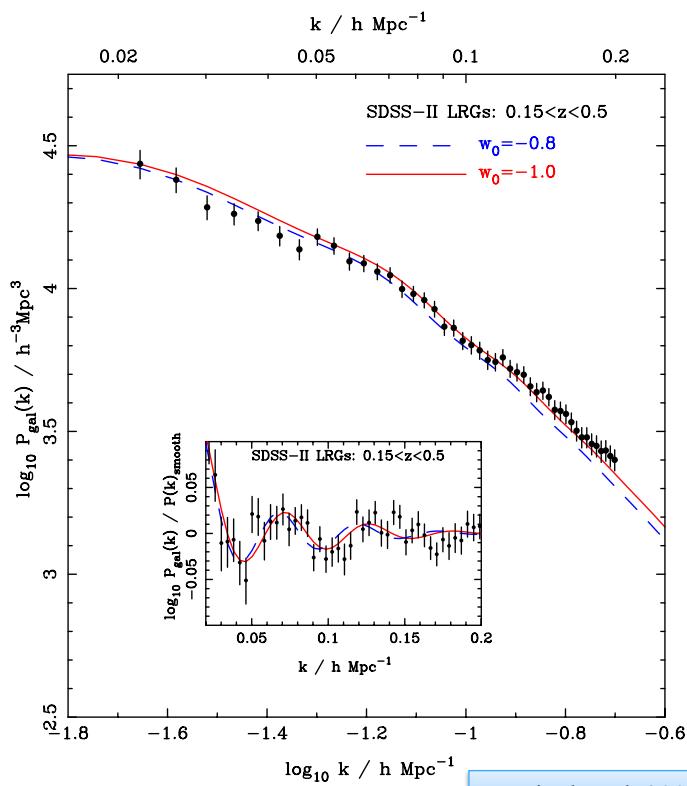
## Current large-scale galaxy clustering measurements

SDSS LRGs at  
 $z \sim 0.35$

The largest volume  
 of the Universe  
 currently mapped

Total effective  
 volume  
 $V_{\text{eff}} = 0.26 \text{ Gpc}^3 \text{h}^{-3}$

Power spectrum  
 gives amplitude of  
 Fourier modes,  
 quantifying  
 clustering strength  
 on different scales

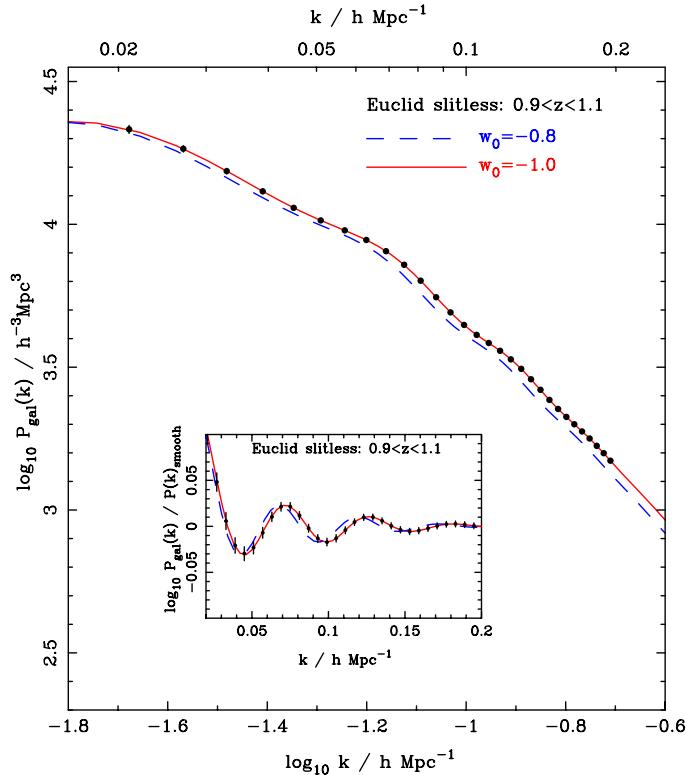


Percival et al. 2009; arXiv:0907.1660

## Predicted galaxy clustering measurements by Euclid

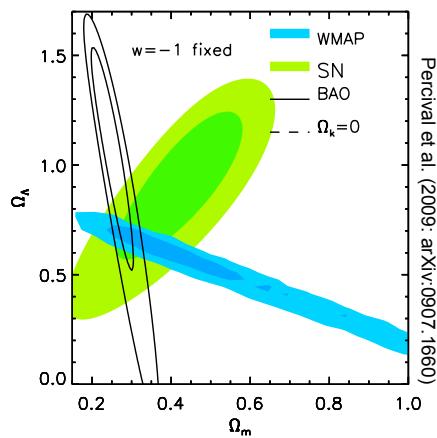
20% of the Euclid  
 data, assuming the  
 slitless baseline at  
 $z \sim 1$

Total effective  
 volume (of Euclid)  
 $V_{\text{eff}} = 19.7 \text{ Gpc}^3 \text{h}^{-3}$

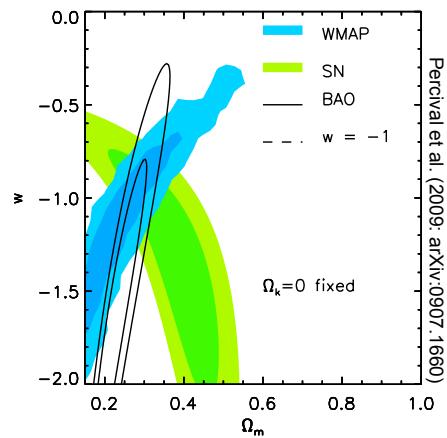


## Current BAO constraints vs other data

$\Lambda$ CDM models with curvature



flat wCDM models

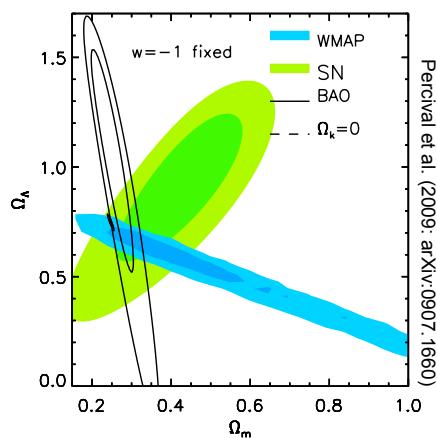


 Union supernovae  
 WMAP 5year  
 SDSS-II BAO Constraint on  $r_s(z_d)/D_V(0.2)$  &  $r_s(z_d)/D_V(0.35)$

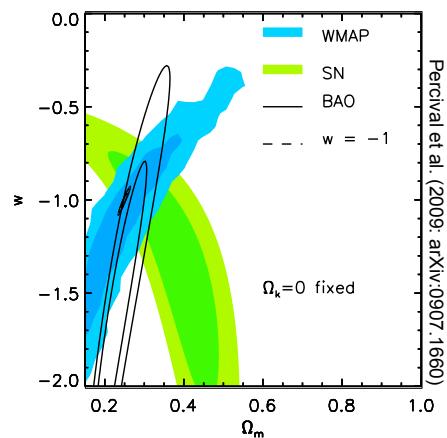
Percival et al. 2009; arXiv:0907.1660

## How does Euclid BAO compare?

$\Lambda$ CDM models with curvature



flat wCDM models



 Union supernovae  
 WMAP 5year  
 SDSS-II BAO Constraint on  $r_s(z_d)/D_V(0.2)$  &  $r_s(z_d)/D_V(0.35)$

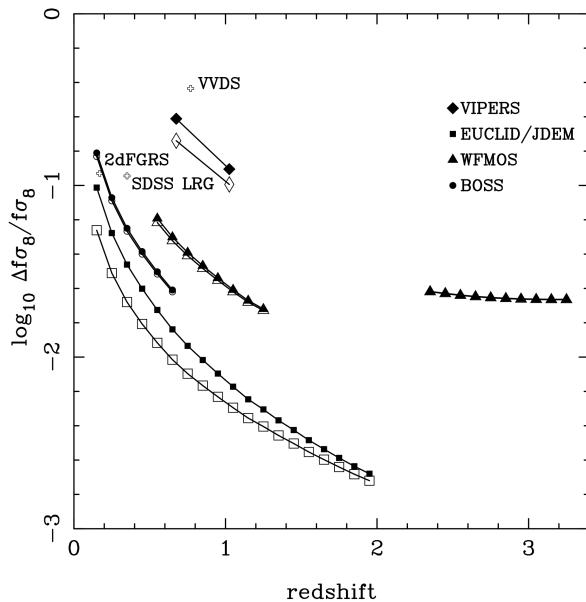
## Fisher matrix prescription

Fisher matrix is statistical tool to translate from errors on parameters that you think you know (e.g.  $P(k)$ ) to errors on parameters that you want to know (e.g.  $f\sigma_8$ ,  $\Omega_m$ ,  $\Omega_b$ ,  $h$ , etc)

For overdensities, can base method on  $\delta$  or  $P(k)$  as the “observed” quantity: give the same result

Code to estimate errors on  $f\sigma_8$  is available from:

<http://mwhite.berkeley.edu/Redshift>



White, Song & Percival, astro-ph/0808.1518

## Summary

- Galaxy clustering in surveys allows us to test cosmological models in many ways
- Smooth shape of the power spectrum?
  - degenerate with galaxy bias
  - bias measurements can tell us about galaxy formation
  - SDSS data shows that galaxy bias is a strong function of luminosity and color
- Baryon acoustic oscillations
  - avoids (almost all of) galaxy bias
  - Already sets interesting constraints on geometry using SDSS
- Redshift-space distortions
  - avoids density bias completely
  - get “for free” for spectroscopic BAO surveys (eg. BOSS)
  - structure formation test so complementary to geometrical tests
  - techniques are currently being advanced
  - similar to weak lensing but tests only temporal metric fluctuations
- Future surveys
  - next generation underway giving an order of magnitude better constraints
  - plans for the next generation of surveys such as Euclid will provide the next leap forwards