

Detection of Superparticles

—

Electroweak Contributions to Squark Pair Production

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Promotionskolloquium

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- 1 Introduction
 - Standard Model and MSSM
 - LHC and Proton–Proton Collisions
 - Squark Pair Production

- 2 Electroweak Contributions
 - Feynman Diagrams
 - Numerical Results
 - Dependence on Transverse Momentum of the Squarks
 - Dependence on Squark Mass
 - Dependence on Gaugino Masses

- 3 Summary

1 Introduction

The Standard Model (SM) of Particle Physics...

- is a relativistic, renormalizable quantum field theory, which based on the gauge group $SU(3)_C \times SU(2)_L \times U(1)_Y$
- describes the **matter particles**, leptons and quarks (an electron is a lepton; a proton consists of three quarks)
- describes **interactions** of the matter particles:
 - electromagnetic interaction (force on charged particles)
 - weak interaction (decay of particles)
 - strong interaction (glue together protons)

Particle content of the Standard Model

- there are **three** generations of quarks and leptons (**spin 1/2**)
- there are **gauge bosons** (**spin 1**), which transfer the interactions
- there is one hypothetical (not yet found) **higgs boson** (**spin 0**), which gives rise to the masses of the particles

Standard Model



(<http://www.hep.ucl.ac.uk/postgrad/>)

BUT, the Standard Model cannot be the “final answer” since it does **NOT**...

- predict neutrino masses
- give an answer to the question why we have three generations of particles
- account for Dark Matter in the Universe
- include the fourth known fundamental interaction, gravity
- ...

Extension of the SM due to **Supersymmetry** (SUSY); SUSY...

- connects fermions (half-integer spin) and bosons (integer spin)
- each SM particle gets a **Superpartner** (“sparticles”),
e.g. quark $q \implies$ squark \tilde{q}
- **simplest** possible realization of SUSY is given within the “**Minimal Supersymmetric extension of the SM**” (MSSM)
- MSSM provides a candidate for Dark Matter, enables the exact unification of the three couplings constants, ...

The MSSM and its particle spectrum

- there is second SU(2)-Higgs doublet with hypercharge $Y = -1$
- SUSY is **not exact**, sparticles do not have the same mass as their SM partners \implies SUSY have to be broken \implies adding soft-terms
- MSSM has **105** extra free parameters
- has "R-parity" conservation, sparticles will be produced always **in pairs**

Names	Boson Fields	Fermion Fields	$SU(3)_C$	$SU(2)_L$	$U(1)_Y$
gluons&gluinos	g^a	\tilde{g}^a	8	0	0
W bosons&winos	W^i	\tilde{W}^i	1	3	0
B boson&bino	B	\tilde{B}	1	1	0
sleptons&leptons	$\tilde{L}^j = (\tilde{\nu}, \tilde{e})_L$	$(\nu, e)_L$	1	2	-1
	$\tilde{E} = \tilde{e}_R^*$	e_R^+	1	1	2
squarks&quarks	$\tilde{Q}^j = (\tilde{u}, \tilde{d})_L$	$(u, d)_L$	3	2	$\frac{1}{3}$
	$\tilde{U} = \tilde{u}_R^*$	u_R^+	3^*	1	$-\frac{4}{3}$
	$\tilde{D} = \tilde{d}_R^*$	d_R^+	3^*	1	$\frac{2}{3}$
Higgs&Higgsinos	H_1^i	$(\tilde{H}_1^0, \tilde{H}_1^-)_L$	1	2	-1
	H_2^i	$(\tilde{H}_2^+, \tilde{H}_2^0)_L$	1	2	1

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Gaugino Mass Eigenstates

particles with **same** $SU(3) \times U(1)_{EM}$ quantum numbers can mix after breaking electroweak symmetry breaking of $SU(2)_L \times U(1)_Y$:

- **charginos** χ_i^\pm are linear combination of charged winos (\tilde{W}^+, \tilde{W}^-) and charged higgsinos ($\tilde{H}_1^-, \tilde{H}_2^+$)
- **neutralinos** χ_i^0 are linear combinations of neutral wino (\tilde{W}^3), bino (\tilde{B}) and neutral higgsinos ($\tilde{H}_1^0, \tilde{H}_2^0$)

mSUGRA

- MSSM has **105 (!)** new parameter \implies work within a **constrained** MSSM: **mSUGRA**, here only **5** free parameter left:
 - $m_0, m_{1/2}$: scalar and gaugino mass
 - A_0 : trilinear coupling
 - $\tan \beta$: ratio of vacuum expectation values of the Higgses
 - $\text{sgn}(\mu)$: sign of the Higgsino mass parameter
- after choice of the five parameters \implies you get masses of the sparticles, parameters for mixing, ...

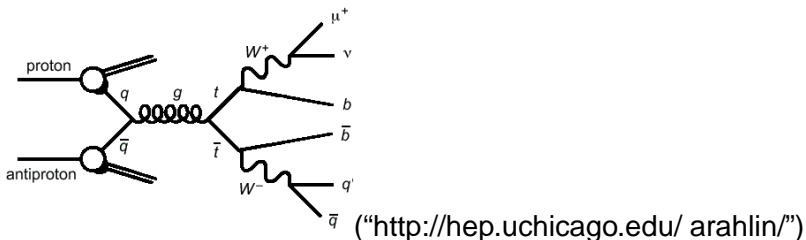
Search for Supersymmetry

- **no** direct experimental evidence for SUSY until now
- expectation that some of the SUSY particles will be found at the Large Hadron Collider (LHC) at CERN:
 - is a proton–proton circular collider
 - is the world's largest particle accelerator (circle of **27km**)
 - is the world's highest–energy particle accelerator ($E_{cm} = 14\text{TeV}$)
 - will be go on line in the end of 2008

(**very**) simplified picture of a proton–proton collision at the LHC:

- one quark of each proton (uud) interact with each other
- probability to find a special quark within a proton is described by so called "parton–distribution functions" (pdf's) $f(x, Q^2)$
- probability for an interaction between two quarks is given by the corresponding cross section $\hat{\sigma}$
- the cross section $\hat{\sigma}$ can be calculated with the help of Feynman diagrams

(very) simplified picture of a p-p collision continue



cross section σ for an process is given by:

$$\sigma = \int dx_1 \int dx_2 f(x_1, \mu^2) f'(x_2, \mu^2) \hat{\sigma}(\hat{s}, \mu^2)$$

- μ : factorization scale
- $f(x_i, \mu^2)$: pdf for proton i ; fraction x_i of the proton energy was given to the corresponding quark
- $\hat{\sigma}(\hat{s}, \mu^2)$ parton cross section for the interaction of the two quarks ($\hat{s} = x_1 x_2 s, \sqrt{\hat{s}} = E_{cm}$)

Squark Pair Production at the LHC

- TeV scale Supersymmetry will be decisively tested at the LHC ($E_{cm} = 14\text{TeV}$)
- squark pairs can be produced via leading order strong interactions
- cross section is $\mathcal{O}(\alpha_s^2)$, e.g.:

$$m_{\tilde{q}} \approx 1000 \text{ GeV}$$

$$\sigma \approx 0.5 \text{ pb}$$

$$\mathcal{L} \approx 10 \text{ fb}^{-1} \text{ per year}$$

$$N_{\text{events}} = \mathcal{L} \sigma$$

- 5000 events are expected at low luminosity

Role of electroweak (EW) contributions

5000 events \Rightarrow

It should be possible to measure the squark pair production cross section with a statistical uncertainty of a few percent.

\Rightarrow

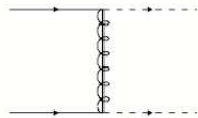
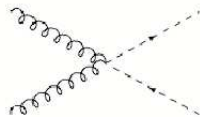
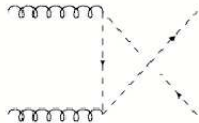
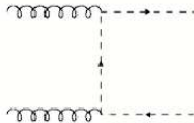
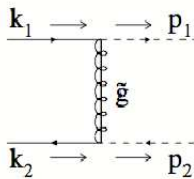
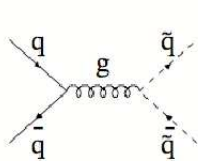
We need accurate theoretical predictions:

- NLO QCD corrections in addition to the LO cross section (Beenakker, Hopker, Spira and Zerwas, 1995)
- remaining uncertainty from yet higher order QCD corrections should be at 10% level

Thus EW corrections at leading order might be important since:

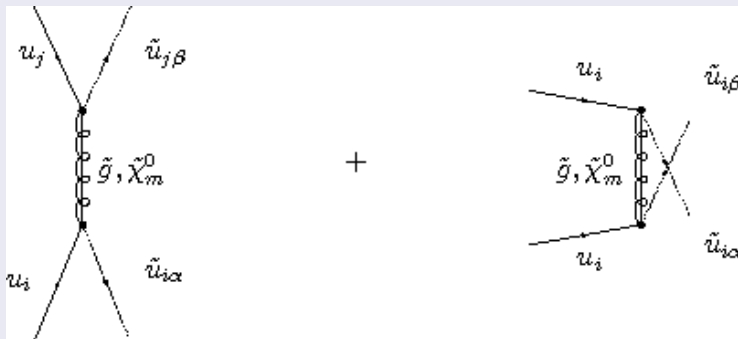
- the interference terms between QCD and EW can be quite sizable
- they can give rise to an increase up to 20% for mSUGRA scenarios and two SU(2) doublet squarks
- they can give rise to an increase up to 50% for scenarios without gaugino mass unification and two SU(2) doublet squarks

QCD: Diagrams for Leading Order Squark Pair Production



2 Electroweak Contributions

$qq' \rightarrow \bar{q}\bar{q}'$: t- or/and u-channel neutralino exchange



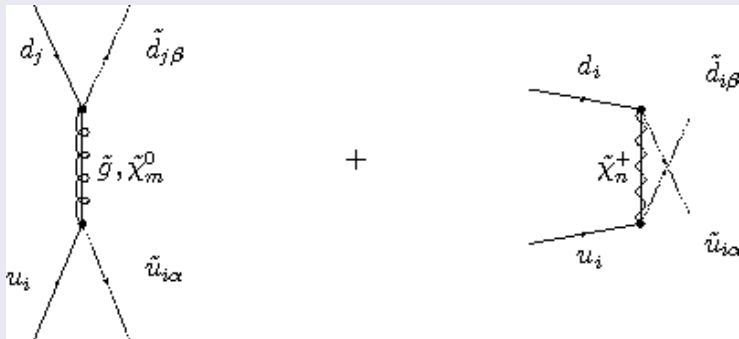
Notation:

- i, j : denotes the generation
- α, β : denotes the chirality (L- and R-type) of the squarks
- m : labels the exchanged neutralino mass eigenstate

Remarks:

- there are **no** s-channel contributions
- there are t- and u-channel ($i=j$) diagrams for neutralino exchange

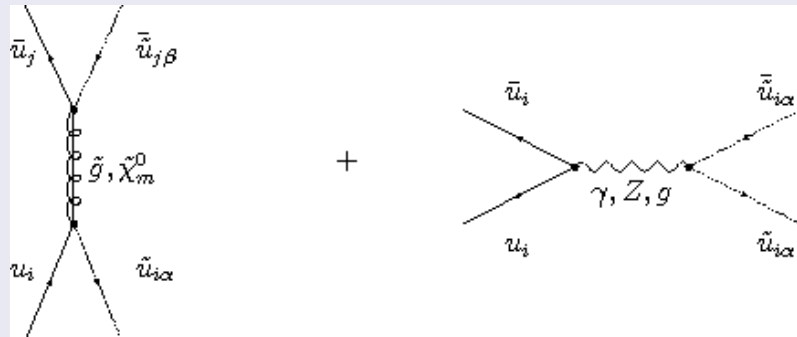
$qq' \rightarrow \tilde{q}\tilde{q}'$: t- or u-channel chargino exchange



Remarks:

- there is **no** gluino u-channel contribution
- u-channel chargino diagrams exist only for $i = j$
- sole chargino t-channel contribution for $u_i d_j \rightarrow \tilde{d}_{i\alpha} \tilde{u}_{j\beta}$ and $i \neq j$

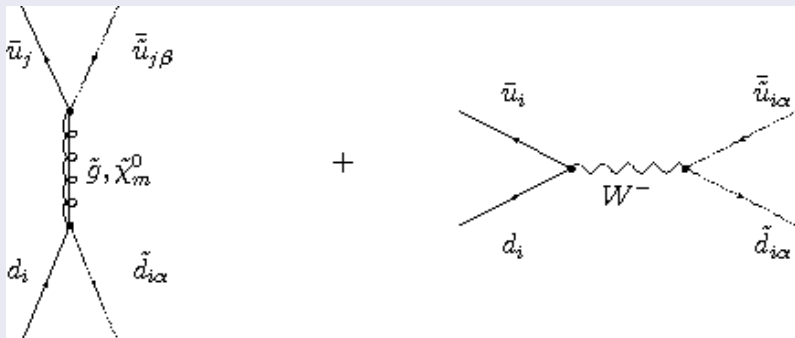
$q\bar{q}' \rightarrow \bar{q}\bar{q}'$: γ, Z, g boson s-channel exchange



Remarks:

- there are s-channel diagrams for $q\bar{q}'$ initial states
- γ, Z, g boson s-channel contributions for $i = j$

$q\bar{q}' \rightarrow \tilde{q}\tilde{q}'$: W boson s-channel exchange

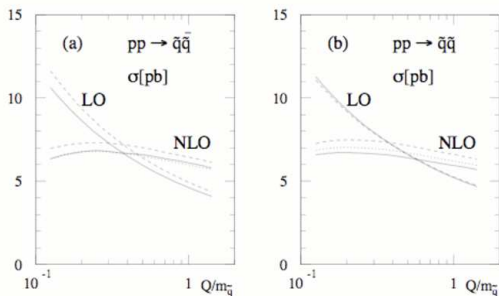


Remarks:

- W boson s-channel contributions for $i = j$
- sole W boson s-channel contribution for $d_i \bar{u}_i \rightarrow \tilde{d}_{j\alpha} \tilde{u}_{j\beta}$ and $i \neq j$

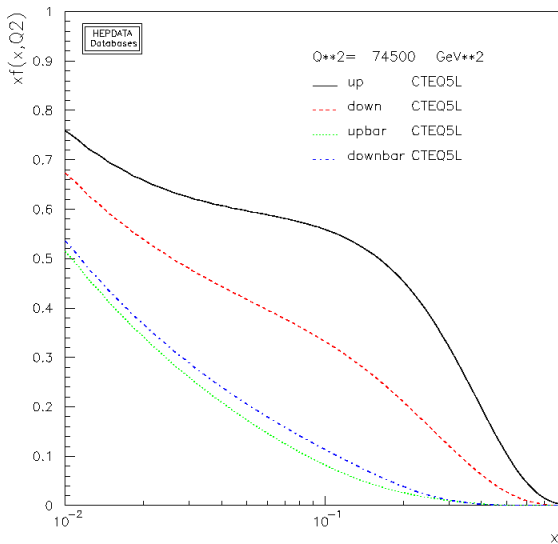
Parameter choice

- we take equal factorization and renormalization scales:
 $\mu_F = \mu_R = m_{\tilde{q}}/2$
- we do **not** consider 3. generation squarks (have no mentionable EW contributions)
- we do **not** consider gluon fusion contributions in the initial states (have no EW contributions in LO)



(Beenakker, Hopker, Spira and Zerwas)

Parton Distribution Functions



(Durham University On-line Plotting and Calculation page)

Numerical Results

Results

mSUGRA	m_0 [GeV]	$m_{1/2}$ [GeV]	$m_{\tilde{q}}$ [GeV]	QCD[pb]		QCD + EW[pb]		ratio	
				Total	LL	Total	LL	Total	LL
SPS 1a	100	250	560	12.11	3.09	12.55	3.50	1.036	1.133
SPS 1b	200	400	865	1.57	0.42	1.66	0.499	1.055	1.186
SPS 2	1450	300	1590	0.055	0.013	0.057	0.0144	1.025	1.091
SPS 3	90	400	845	1.74	0.464	1.83	0.551	1.055	1.188
SPS 4	400	300	760	3.10	0.813	3.22	0.927	1.040	1.141
SPS 5	150	300	670	5.42	1.41	5.66	1.62	1.042	1.152

Remarks

- EW contribution is more important for two SU(2) doublet squarks, due to $(g_2/g_Y)^2 = \cot^2 \theta_w \approx 3.3$
- EW contribution depends on the ratio $m_{1/2}/m_0$
- EW contribution becomes more important for heavier squarks if ratio $m_0/m_{1/2}$ remains roughly the same

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- EW contribution is more important for two SU(2) doublet squarks, due to $(g_2/g_Y)^2 = \cot^2 \theta_w \approx 3.3$
- EW contribution depends on the ratio $m_{1/2}/m_0$
- EW contribution becomes more important for **heavier** squarks if ratio $m_0/m_{1/2}$ remains roughly the same

Helicity flip and threshold behaviour:

Processes like $u_L u_L \rightarrow \tilde{u}_L \tilde{u}_L$:

- matrix element is proportional to **mass** of exchanged gaugino (helicity flip)
- both quarks have to be left-handed \implies total momentum $J = 0$; squarks are in a s-wave
- $\sigma_{\text{total}} \propto \beta$,

$$\text{where } \beta = v = \frac{p}{E} = \sqrt{1 - \frac{4m_{\tilde{q}}^2}{\hat{s}}}$$

Processes like $u_L u_R \rightarrow \tilde{u}_L \tilde{u}_R$:

- matrix element is **NOT** proportional to mass of exchanged gaugino (no helicity flip)
- addition of right- and left-handed quark \implies total momentum $J = 1$; squarks are in a p-wave
- $\sigma_{\text{total}} \propto \beta^3$

Electroweak Contributions, 1st category:

No.	Process	diagrams		helicity flip?	threshold	cross section [pb]		ratio
		QCD	EW			QCD	QCD + EW	
1	$uu \rightarrow \tilde{u}_L \tilde{u}_L$	t, u	t, u	yes	β	0.683	0.794	1.162
2	$uu \rightarrow \tilde{u}_R \tilde{u}_R$	t, u	t, u	yes	β	0.761	0.796	1.045
3	$uu \rightarrow \tilde{u}_L \tilde{u}_R$	t, u	t, u	no	β^3	0.929	0.931	1.002
4	$dd \rightarrow \tilde{d}_L \tilde{d}_L$	t, u	t, u	yes	β	0.198	0.232	1.171
5	$dd \rightarrow \tilde{d}_R \tilde{d}_R$	t, u	t, u	yes	β	0.234	0.237	1.012
6	$dd \rightarrow \tilde{d}_L \tilde{d}_R$	t, u	t, u	no	β^3	0.243	0.243	1.000
7	$ud \rightarrow \tilde{u}_L \tilde{d}_L$	t	t, u	yes	β	0.969	1.22	1.261

- possible interference between t- and u-channel diagrams
- processes with two SU(2) doublet squarks have:
 - constructive (positive) interference terms between QCD and EW
 - helicity flip, so $\sigma \propto \beta$ and $\mathcal{M} \propto M_{\tilde{G}}$
- cross sections are sizable due to two valence quarks

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Electroweak Contributions, 2nd category:

No.	Process	diagrams		helicity flip?	threshold	cross section [pb]		ratio
		QCD	EW			QCD	QCD + EW	
8	$u\bar{u} \rightarrow \tilde{u}_L \tilde{u}_L$	s, t	s, t	no	β^3	0.165	0.140	0.848
9	$u\bar{u} \rightarrow \tilde{u}_R \tilde{u}_R$	s, t	s, t	no	β^3	0.187	0.170	0.909
10	$d\bar{d} \rightarrow \tilde{d}_L \tilde{d}_L$	s, t	s, t	no	β^3	0.0925	0.0784	0.847
11	$d\bar{d} \rightarrow \tilde{d}_R \tilde{d}_R$	s, t	s, t	no	β^3	0.109	0.106	0.972
12	$u\bar{u} \rightarrow \tilde{d}_L \tilde{d}_L$	s	s, t	no	β^3	0.0341	0.0353	1.035
13	$d\bar{d} \rightarrow \tilde{u}_L \tilde{u}_L$	s	s, t	no	β^3	0.0207	0.0219	1.057
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18	$u\bar{u} \rightarrow \tilde{u}_L \tilde{u}_R$	t	t	yes	β	0.569	0.569	1.000
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Dependence on transverse momentum p_T of the squarks

Ratio of EW and QCD t- or u-channel propagator is given by

$$\frac{EW}{QCD} \approx \frac{2p_T^2 + m_{\tilde{q}}^2 + M_{\tilde{g}}^2}{2p_T^2 + m_{\tilde{q}}^2 + M_{\tilde{W}}^2},$$

where

- p_T is the transverse momentum of the squarks
- $m_{\tilde{q}}/m_{\tilde{g}}$ is the squark/gluino mass
- $M_{\tilde{W}}$ is the relevant chargino or neutralino mass

Therefore:

- enhancement by a factor of 2 for small p_T for $m_{\tilde{q}} \approx M_{\tilde{g}} \gg M_{\tilde{W}}$ (nearly all SPS scenarios)
- enhancement vanishes for $2p_T^2 \gg m_{\tilde{q}}^2$
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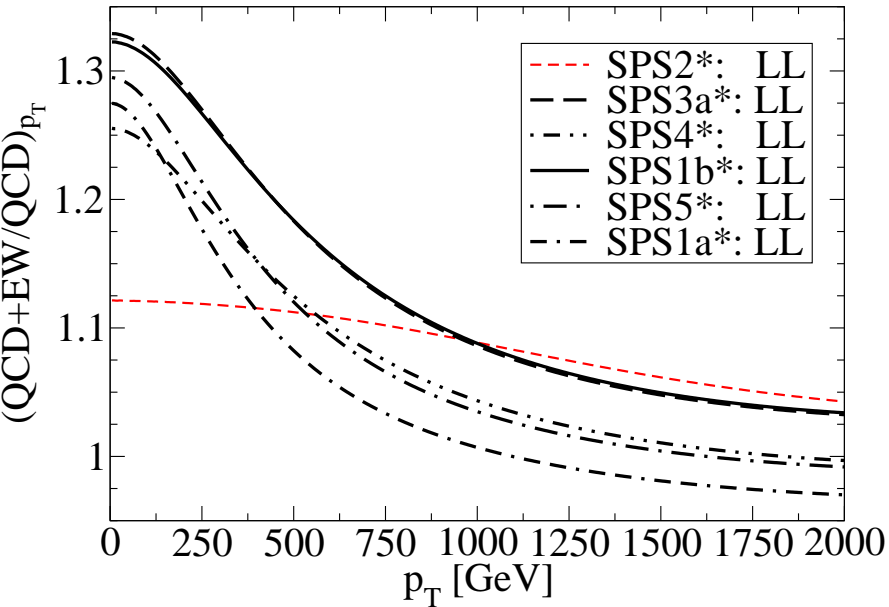
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Dependence on squark mass

Larger squark masses give rise to:

- smaller values of β due to reduction of the phase space

$$\beta = \sqrt{1 - \frac{4m_{\tilde{q}}^2}{\hat{s}}}$$

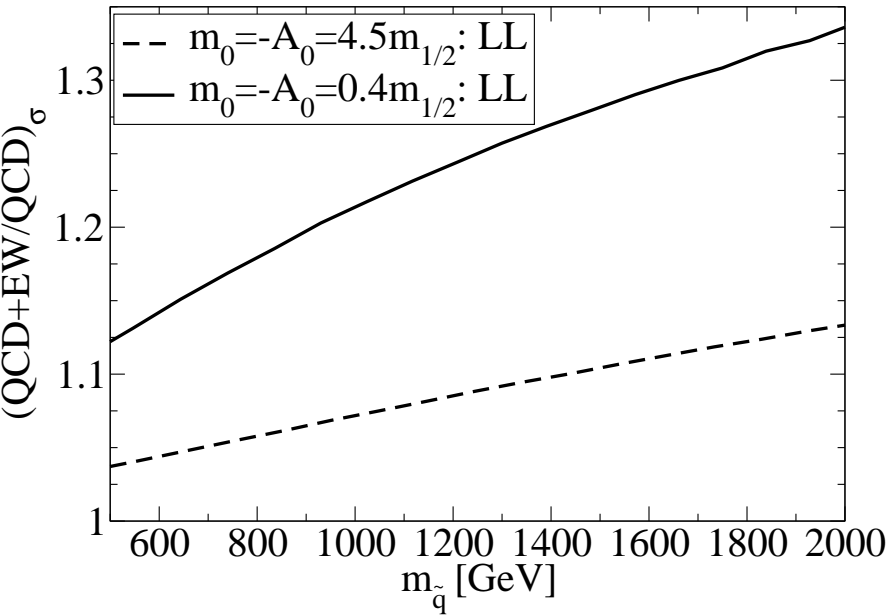
- anti-quarks suffer higher suppression than quarks (Bjorken-x)

$$\hat{s} = 4 \left(m_{\tilde{q}}^2 + \frac{p_T^2}{\sin^2 \theta} \right), \hat{s} = x_1 x_2 s$$

So larger squark masses lead to:

- higher suppression of the destructive interference terms of category 2, which have an **anti-quark** and $\sigma \propto \beta^3$
- nearly all processes of category 3 have anti-quark or/and $\sigma \propto \beta^3$ suppressions

\Rightarrow **higher weighting** of the positive contributions



Dependence on gaugino masses

- category 1 \propto to $M_{\tilde{g}}M_{\tilde{W}}$, so sensitive to ratio of gaugino masses
- in mSUGRA:

$$M_1 : M_2 : M_3 \sim 1 : 2 : 7 \text{ at the weak scale}$$

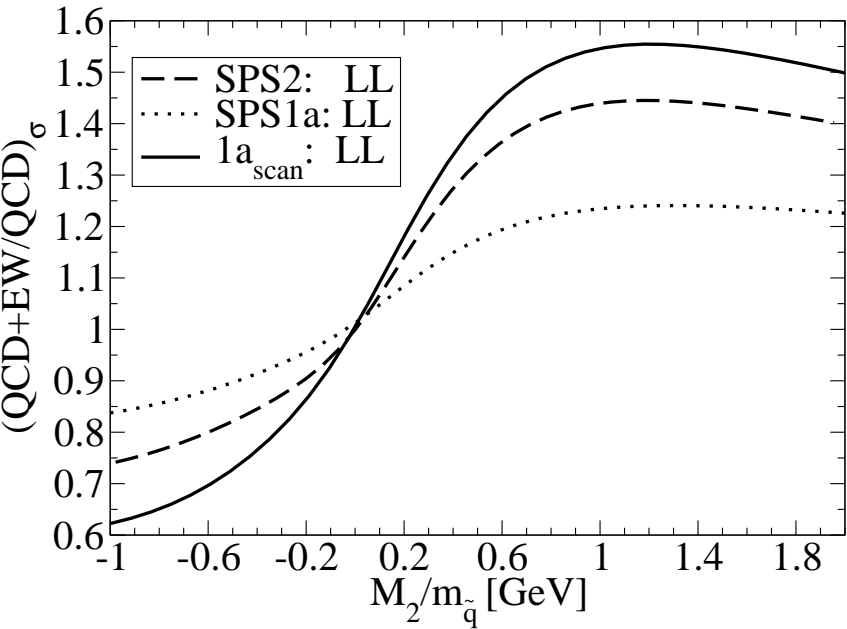
\Rightarrow larger EW contributions **without** gaugino mass unification

For example, **vary M_2** at the weak scale:

- maximum of curve is at $M_2 = m_{\tilde{g}}$, since it maximizes

$$\frac{M_2}{\hat{t} - M_2^2}$$

- $M_2 < 0$ (keep sign of $M_{\tilde{g}}$) leads to negative EW contributions due to change of the sign of the interference terms of category 1



3 Summary

Summary

- MSSM: each SM particle gets a superpartner
- TeV scale SUSY will be tested at the LHC
- squark pair production will be important; determination of the production cross section with a high precision
- even leading order EW contributions might be important
- EW correction increases with the squark mass
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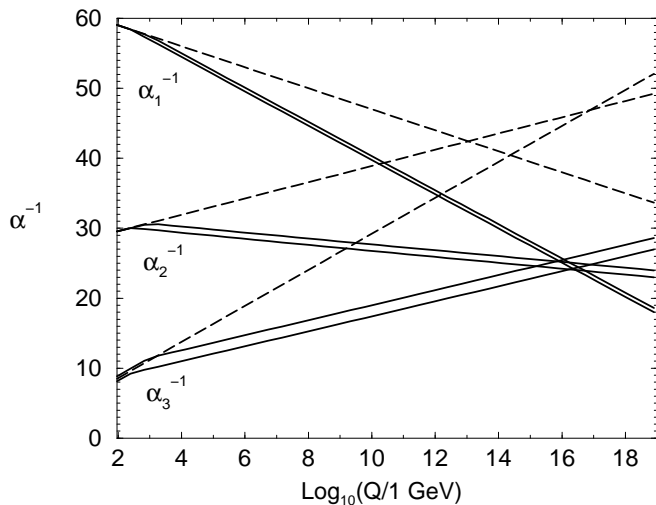
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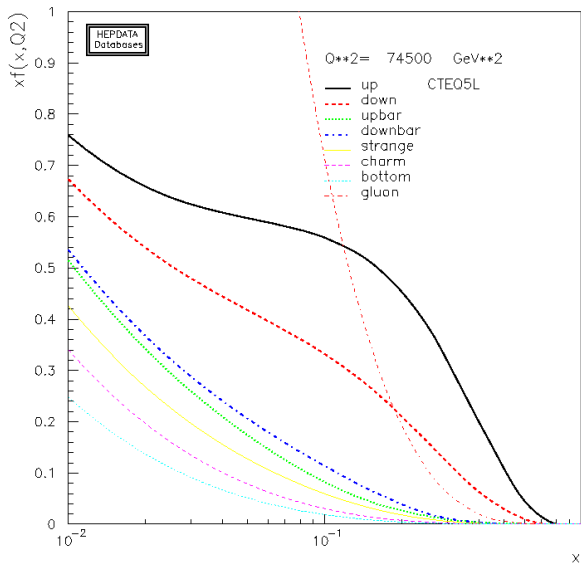
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- **Thank you!! Questions?!**

Backup Slides

Gauge coupling unification

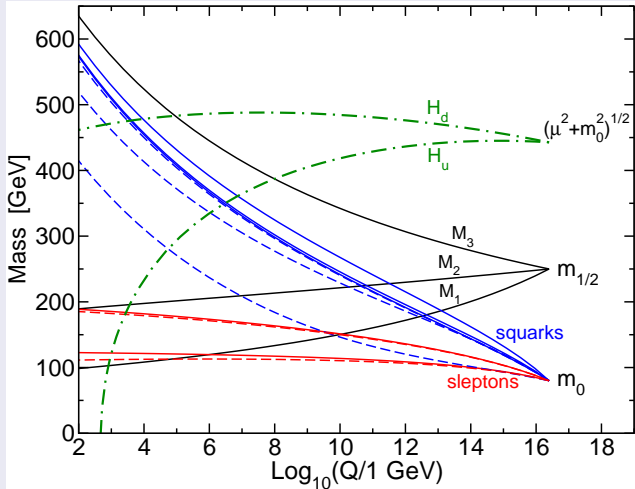


Parton Distribution Functions

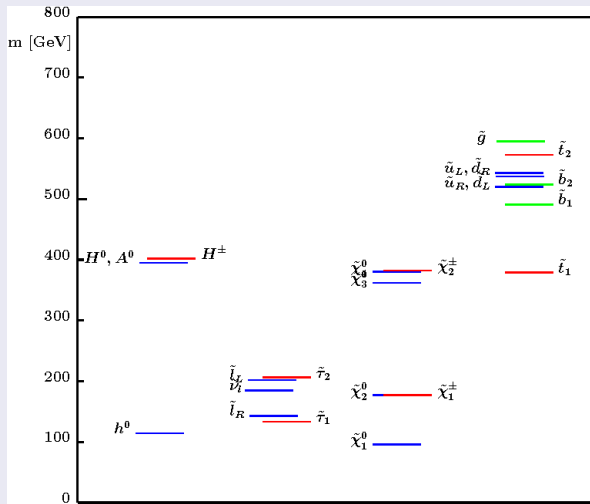


(Durham University On-line Plotting and Calculation page)

mSUGRA



Mass eigenstates



Dependence on p_T continue

There are three cases of decrease for large p_T ; why?!:

- interference terms of category 1:

$$\propto M_{\tilde{g}} M_{\tilde{W}} \quad (\text{helicity flip}),$$

this has to be compensated by an extra factor of p_T^{-2} for large p_T

- negative interference terms of category 2 (no helicity flip) have suppression for large p_T due to anti-quark in the initial state

$$\hat{s} = 4 \left(m_{\tilde{q}}^2 + \frac{p_T^2}{\sin^2 \theta} \right), \hat{s} = \mathbf{x} \mathbf{s}$$

Thus:

- category 1 and 2 have **competing** suppressions factors
- for the three cases: category 2 dominates slightly
- larger suppression of category 2 for larger squark masses

Dependence on squark mass continue

Two further observations:

- increase of the cross section can be much different for a fixed squark mass
- maximal relative size of EW contributions larger than the most favorable single process of category 1

For **smaller** squark masses (larger β) the weighting of processes with **squared** t-channel and u-channel propagators is **higher**:

- t-channel propagator is given by

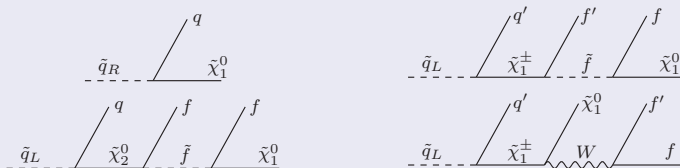
$$\frac{1}{\hat{t} - M_{\tilde{q}}^2} = \frac{1}{m_{\tilde{q}}^2 - \frac{\hat{s}}{2}(1 - \beta \cos \theta) - M_{\tilde{g}}^2},$$

⇒ highest contributions for **large** $|\beta \cos \theta|$

- **pure** QCD gives largest contributions to processes with non-mixed propagators (for u-channel replace $\cos \theta \rightarrow -\cos \theta$)
- pure QCD interference terms (mixed propagators) are destructive

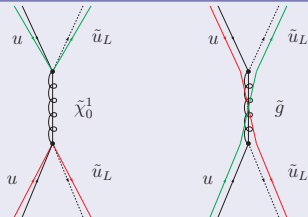
Signal I

- EW contribution is much smaller for SU(2) singlet final states
- for $m_{\tilde{g}} > m_{\tilde{q}} > |M_2|, |M_1|$
- SU(2) doublets decay into charginos and neutralinos dominated by SU(2) gaugino components, in mSUGRA: $\tilde{\chi}_2^0$ and $\tilde{\chi}_1^\pm$
- SU(2) singlets decay into bino-like neutralinos, in mSUGRA: $\tilde{\chi}_1^0$



- the rate for doublet squarks can therefore be experimentally enhanced by the presence of energetic, isolated charged leptons, ≥ 2 jets and missing transverse momentum

Rapidity gaps



- in EW channels, both partons are not color-connected
- if both jets are not color-connected, gluons will fill the phase space between the jets and the beam remnants
- if both jets are color-connected, the phase space between both jets will be filled by gluons