

Constraints on the very early universe from thermal WIMP Dark Matter

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In collaboration with

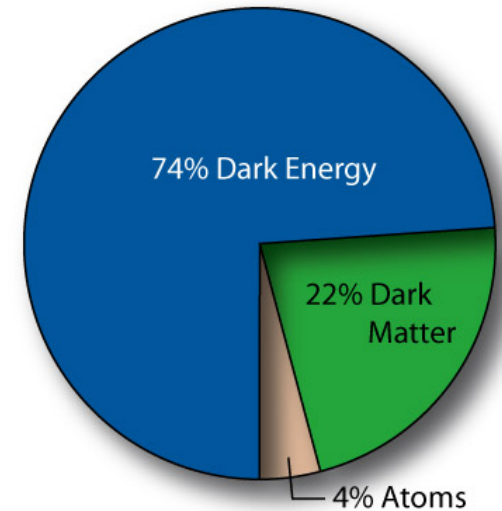
- Manuel Drees
- Hoernisa Iminniyaz

Refs:

- PRD73 (2006) 123502 [hep-ph/0603165]
- arXiv:0704.1590 [hep-ph]

1. Motivation

- Observations of
 - cosmic microwave background
 - structure of the universe
 - etc.



[<http://map.gsfc.nasa.gov>]

➔ Non-baryonic cold dark matter (CDM): $0.8 < \Omega_{\text{CDM}} h^2 < 0.12$ (95% CL)

- Neutral, stable (long-lived) weakly interacting massive particles (WIMPs) χ are good candidates for CDM
 - Neutralino (LSP); 1st KK mode of the B boson (LKP); etc.

When WIMPs were in full thermal eq., the relic abundance naturally falls around the observed CDM abundance: $\Omega_{\chi, \text{standard}} h^2 \sim 0.1$

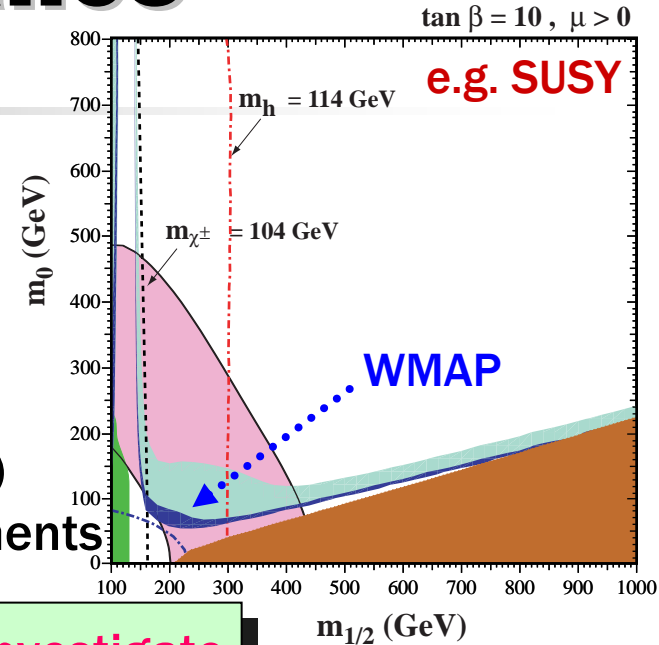
Investigation of early universe using CDM abundance

- The relic abundance of thermal WIMPs is determined by the Boltzmann equation:

$$\dot{n}_\chi + 3Hn_\chi = -\langle\sigma_{\text{eff}}v\rangle(n_\chi^2 - n_{\chi,\text{eq}}^2)$$

(and the reheat temperature: T_R)

- The (effective) cross section σ_{eff} can be (hopefully) determined from collider and DM detection experiments



→ We can test the standard CDM scenario and investigate the conditions of very early universe: T_R, H, \dots

[From Ellis et al., PLB565 (2003) 176]

- Standard scenario:

- χ was in chemical eq.

$\Omega_\chi h^2$ is independent of T_R

- $H = \frac{\pi T^2}{M_{\text{Pl}}} \sqrt{\frac{g_*}{90}}$ (g_* : Rel. dof)

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- Non-standard scenarios:

- Low reheat temperature

- Entropy production

- Modified Hubble parameter

- Non-thermal production

[Scherrer et al., PRD(1985);
Salati, PLB(2003);
Fernengo et al., PRD(2003); Chung et al., PRD (1999); ...]

Outline

This work

- We provide an approximate analytic treatment that is applicable to low-reheat-temperature scenarios
- Based on the assumption of CDM = thermal WIMP
 - we derive the lower bound on the maximal temperature of RD epoch
 - we constrain possible modifications of the Hubble parameter

c.f. Cosmic p^+, γ  Bounds on pre-BBN expansion

[Schelke, Catena, Fornengo, Masiero, Pietroni PRD74 (2006);
Donato, Fornengo, Schelke, JCAP0703 (2007)]

1. Motivation
2. Standard calculation of WIMP relic abundance
3. Low-temperature scenario
4. Constrains on the very early universe from WIMP dark matter
5. Summary

2. Standard calculation of the WIMP relic abundance

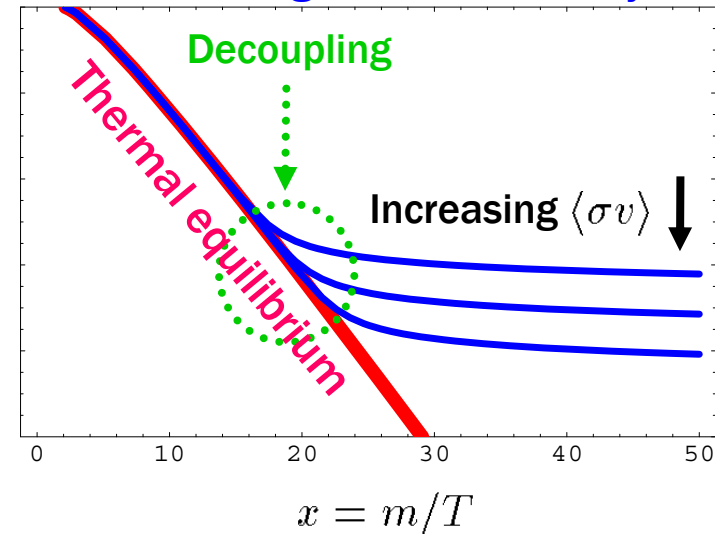
[Scherrer, Turner, PRD33(1986); Griest, Seckel, PRD43(1991); ...]

- Conventional assumptions for χ :
 - $\chi = \bar{\chi}$, single production of χ is forbidden
 - Thermal equilibrium was maintained
- For adiabatic expansion the Boltzmann eq. is

$$\frac{dY_\chi}{dx} = -\frac{\langle\sigma v\rangle s}{Hx} (Y_\chi^2 - Y_{\chi,\text{eq}}^2),$$

$$Y_{\chi(\text{,eq})} = \frac{n_{\chi(\text{,eq})}}{s}, \quad x = \frac{m_\chi}{T}$$

Co-moving number density



- During the RD epoch, χ and decoupled when they were non-relativistic:

$$\langle\sigma v\rangle = a + 6b/x + \mathcal{O}(1/x^2), \quad n_{\chi,\text{eq}} = g_\chi (m_\chi T/2\pi)^{3/2} e^{-m_\chi/T}$$

→
$$\Omega_{\chi,\text{standard}} h^2 \simeq 0.1 \times \left(\frac{a + 3b/x_F}{10^{-9} \text{ GeV}^{-2}} \right)^{-1} \left(\frac{x_F}{22} \right) \left(\frac{g_*}{90} \right)^{-1/2} \sim \Omega_{\text{CDM}} h^2$$



3. Low-temperature scenario

- T_R : Reheat temperature

The initial abundance is assumed to be negligible: $Y_\chi(x_0) = 0$, $x_0 = \frac{m_\chi}{T_R}$

- Zeroth order approximation:

$T_R < T_F$ \rightarrow χ annihilation is negligible:

$$\frac{dY_0}{dx} = 0.028 g_\chi^2 g_*^{-3/2} m_\chi M_{\text{Pl}} e^{-2x} x \left(a + \frac{6b}{x} \right)$$

\rightarrow The solution is proportional to the cross section:

At late times,

$$Y_0(x \gg x_0) \simeq 0.014 g_\chi^2 g_*^{-3/2} m_\chi M_{\text{Pl}} e^{-2x_0} x_0 \left(a + \frac{6b}{x_0} \right)$$

This solution should be smoothly connected to the standard result

First order approximation

- Add a correction term describing annihilation to Y_0 : $Y_1 = Y_0 + \delta$ ($\delta < 0$)
- As long as $|\delta| \ll Y_0$, the evolution equation for δ is

$$\frac{d\delta}{dx} = -1.3 \sqrt{g_*} m_\chi M_{\text{PL}} \left(a + \frac{6b}{x} \right) \frac{Y_0(x)^2}{x^2}$$

➡ The solution is proportional to σ^3

At late times,

$$\delta(x \gg x_0) \simeq -2.5 \times 10^{-4} g_\chi^4 g_*^{-5/2} m^3 M_{\text{Pl}}^3 e^{-4x_0} x_0 \left(a + \frac{3b}{x_0} \right) \left(a + \frac{6b}{x_0} \right)^2$$

- $|\delta|$ soon dominates over Y_0 for not very small cross section

➡ Y_1 fails to track the exact solution

Re-summed ansatz

- It is noticed that $Y_0 \propto \sigma > 0$, $\delta \propto \sigma^3 < 0$

For large cross section,

$Y_\chi(x \rightarrow \infty)$ should be $\propto 1/\langle \sigma v \rangle$

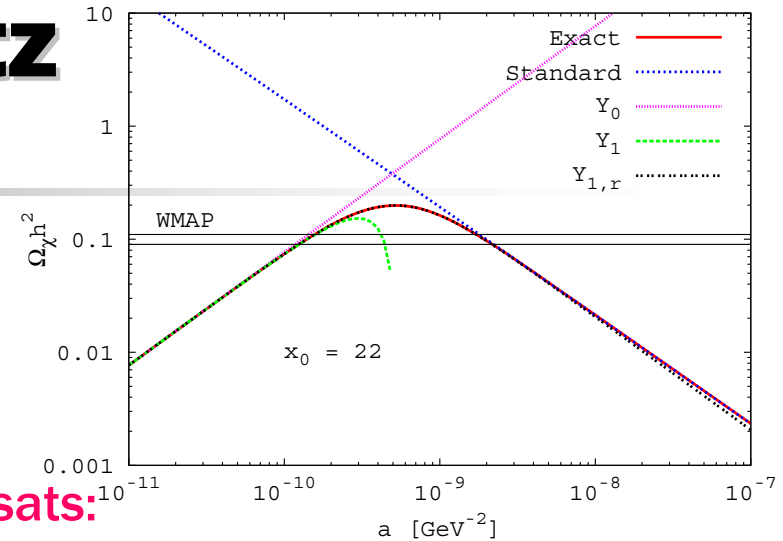
- This observation suggests the re-summed ansatz:

$$Y(x) = Y_0 + \delta = Y_0 \left(1 + \frac{\delta}{Y_0} \right) \simeq \frac{Y_0}{1 - \delta/Y_0} \equiv Y_{1,r}$$

- For $|\delta| \gg Y_0$, $Y_{1,r}(x) \simeq -\frac{Y_0^2}{\delta} \propto \frac{1}{\sigma}$

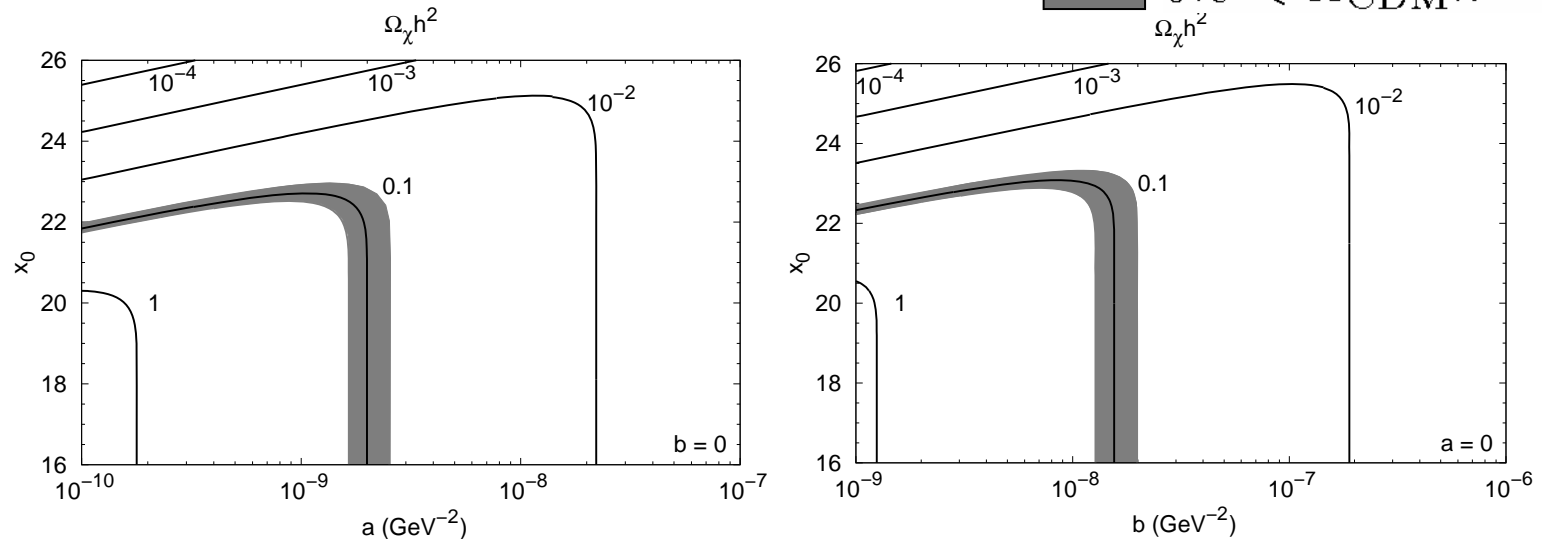
At late times, $Y_{1,r}(x \rightarrow \infty) = \frac{x_0}{1.3 \sqrt{g_*} m_\chi M_{\text{Pl}} (a + 3b/x_0)}$

- In the case where χ production is negligible but the initial abundance is sizable, $Y_{1,r}$ is exact



4. Constrains on the very early universe from WIMP DM

- Out-of-equilibrium case: $\sigma \nearrow \Rightarrow \Omega h^2 \nearrow$; $T_0 = m_\chi/x_0 \nearrow \Rightarrow \Omega h^2 \nearrow$
- Equilibrium case: $\sigma \nearrow \Rightarrow \Omega h^2 \searrow$; Ωh^2 Independent of T_0
- Thermal relic abundance in the RD universe: $0.8 < \Omega_{\text{CDM}} h^2 < 0.12$



Assumption of $\Omega_{\text{CDM}} h^2 = \Omega_{\chi, \text{thermal}} h^2$,
 \Rightarrow Lower bound on the maximal temperature: $T_R > m_\chi/23$

Modified expansion rate

- Various cosmological models predict a non-standard early expansion
 [e.g. Scherrer et al.,PRD(1985); Salati,PLB(2003);
 Ferrigno et al.,PRD(2003); Chung et al., PRD (1999); ...]
- ➡ Predicted WIMP relic abundances are also changed
- When WIMPs were in full thermal equilibrium, in terms of the modification parameter $A(x) = H_{\text{st}}(x)/H(x)$ the relic abundance is

$$\Omega_\chi h^2 = 0.1 \left(\frac{I(x_F)}{8.5 \times 10^{-10} \text{ GeV}^{-2}} \right)^{-1}$$

$$I(x_F) = \int_{x_F}^{\infty} dx \frac{\sqrt{g_*} \langle \sigma v \rangle A(x)}{x^2}, \quad x_F = \ln \left[\sqrt{\frac{45}{\pi^5}} \xi m_\chi M_{\text{Pl}} g_\chi \frac{\langle \sigma v \rangle A(x)}{\sqrt{x g_*}} \right] \Big|_{x=x_F}$$

If $A(x) = 1$, $x_F = x_{F,\text{st}}$ and we recover the standard formula

This formula is capable of predicting the final relic density correctly

Constraints on modifications of the Hubble parameter

- In terms of $z \equiv T/m_\chi = 1/x$

we need to know $A(z)$ only for $z_{\text{BBN}} = 10^{-5} - 10^{-4} \leq z \leq z_F \sim 1/20 \ll \mathcal{O}(1)$

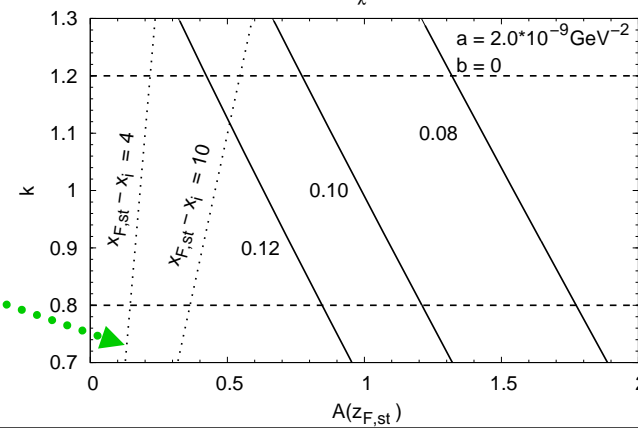
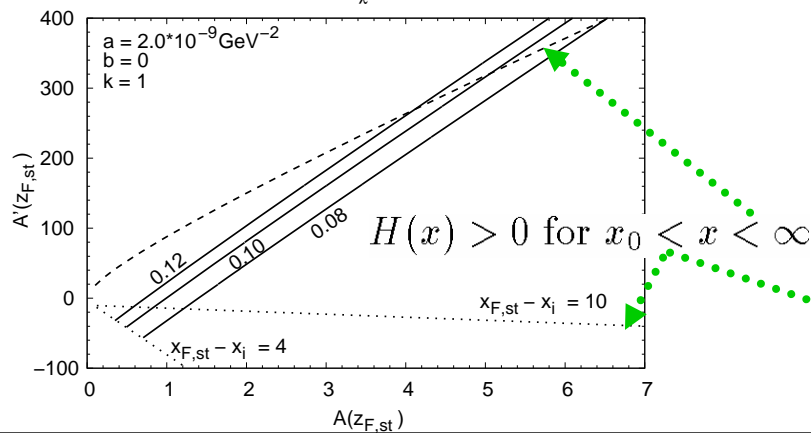
→ This suggests a parametrization of $A(z)$ in powers of $(z - z_{F,\text{st}})$:

$$A(z) = A(z_{F,\text{st}}) + (z - z_{F,\text{st}})A'(z_{F,\text{st}}) + \frac{1}{2}(z - z_{F,\text{st}})^2 A''(z_{F,\text{st}})$$

subject to the BBN limit: $0.8 \leq k \equiv A(z \rightarrow z_{\text{BBN}}) \leq 1.2$

- Once we know σ_χ , we can constrain $A(z)$:

x_i : Maximal temperature where the parametrization is valid



$\Omega_\chi h^2$ depends on all $H(T_{\text{BBN}} < T < T_F)$ → Larger allowed region for $H(T_F)$



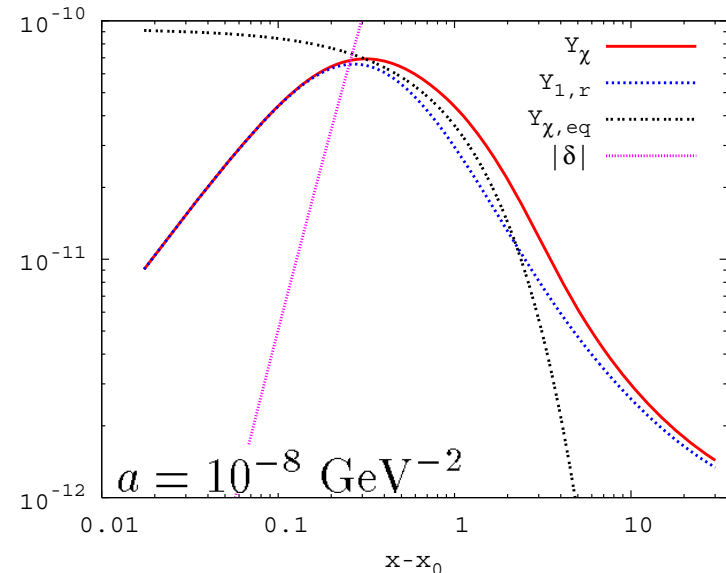
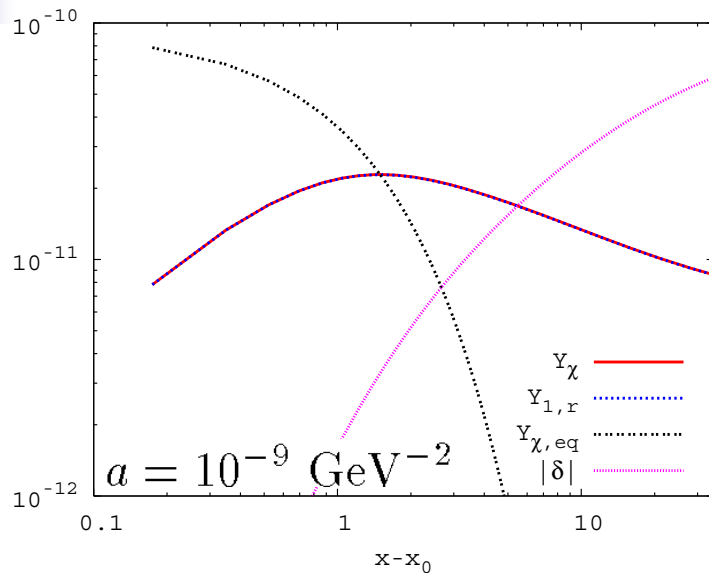
5. Summary

- Using the CDM relic density we can examine very early universe around $T \sim m_\chi/20 \sim \mathcal{O}(10)$ GeV (well before BBN $T_{\text{BBN}} \sim \mathcal{O}(1)$ MeV)
- The relic density of thermal WIMPs depends on the reheat temperature T_R and on the Hubble parameter $H(T_{\text{BBN}} < T < T_F)$
- By applying $\Omega_{\text{CDM}} h^2 = \Omega_{\chi, \text{thermal}} h^2$, we found the lower bound on the maximal temperature: $T_R > m_\chi/23$
- The sensitivity of $\Omega_{\chi, \text{thermal}} h^2$ on $H(T_F)$ is weak because $\Omega_{\chi, \text{thermal}} h^2$ depends on all $H(T_{\text{BBN}} < T < T_F)$



Backup slides

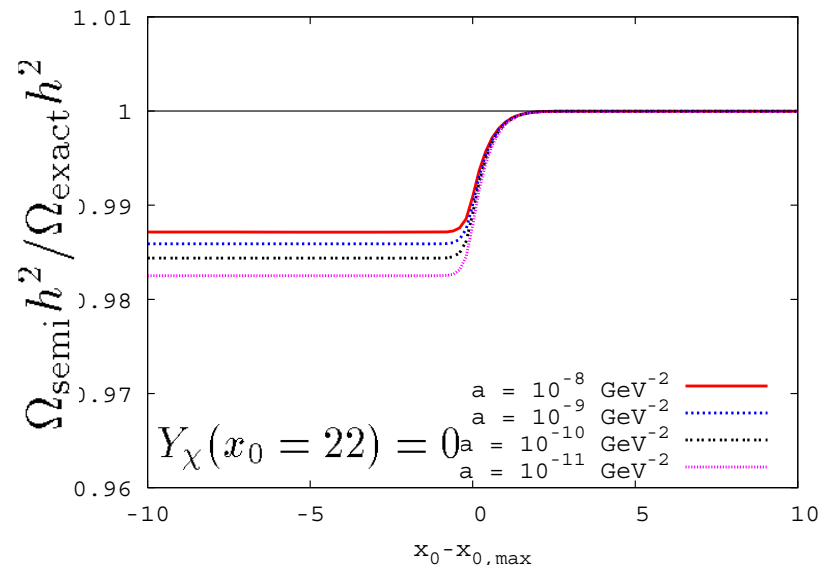
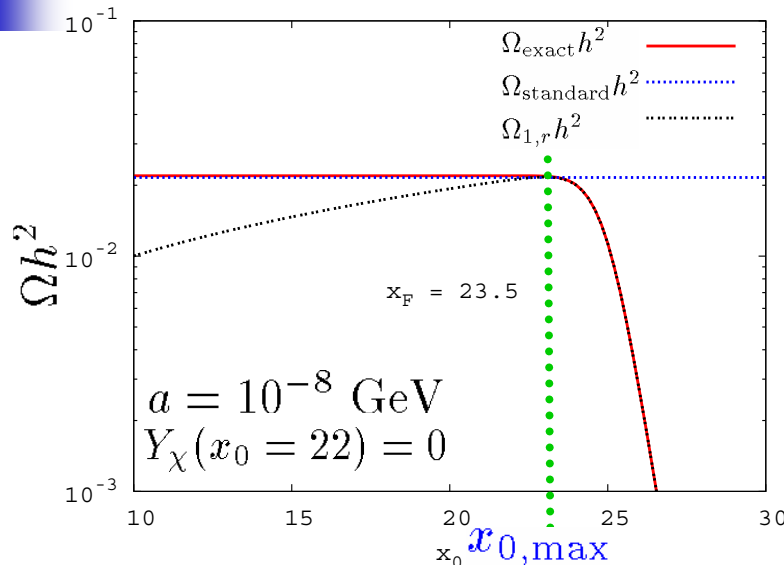
Evolution of solutions



Y_χ : Exact result, $Y_{1,r}$: Re-summed ansatz, $b = 0$, $Y_\chi(x_0 = 22) = 0$

- The re-summed ansatz $Y_{1,r}$ describes the full temperature dependence of the abundance when equilibrium is not reached
- For larger cross section the deviation becomes sizable for $x - x_0 \sim 1$, but the deviation becomes smaller for $x \gg x_0$

Semi-analytic solution



- $Y_{1,r}(x_0, x \rightarrow \infty) (\propto \Omega_{1,r} h^2)$ has a maximum (left)
- New semi-analytic solution can be constructed: $\Omega_{\text{semi}} h^2$ (right)

For $x_0 > x_{0,\text{max}}$, use $Y_{1,r}(x_0)$; for $x_0 < x_{0,\text{max}}$, use $Y_{1,r}(x_{0,\text{max}})$

The semi-analytic solution $\Omega_{\text{semi}} h^2$ reproduces the correct final relic density $\Omega_{\text{exact}} h^2$ to an accuracy of a few percent