

Green–Schwarz Mechanism in Heterotic (2,0) GLSMs

Torsion and NS5 Branes

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String Phenomenology 2011 – 08/24/2011



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Based on: [Blaszczyk,Groot Nibbelink,FR: 1107.0320]

(see also: [Quigley,Sethi])

Motivation

String theory promising candidate for unified description of **fundamental forces**.

Much effort spent on construction of **MSSM**-like models in last decade.

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Approaches in $E_8 \times E_8$ heterotic string theory:

- **Orbifold** model building [Blaszczyk, Buchmüller, Groot Nibbelink, Hamaguchi, Kim, Kyaе, Lebedev, Nilles, Raby, Ramos–Sanchez, Ratz, FR, Trapletti, Vaudrevange, Wingerter, . . .]
- **Calabi–Yau** model building [Anderson, Bouchard, Braun, Donagi, Gray, He, Lukas, Ovrut, Palti, Pantev, Waldram, . . .]
- **Free fermionic** constructions [Faraggi, Nanopoulos, Yuan, . . .]
- **Gepner Models** [Dijkstra, Gato–Rivera, Huiszoon, Schellekens, . . .]

Motivation – Compactification Geometries



Orbifold

singular, non-generic



Calabi-Yau

smooth, generic

Motivation – Compactification Geometries



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exact **CFT** calculations possible



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only **SUGRA approximation**

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singular, non-generic

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exact **CFT** calculations possible

Anomaly **drives** model **away**
from **Orbifold** point

smooth, generic

complicated

only **SUGRA** approximation

Phenomenology (torsion) **drives**
model **away** from **CY** space

Motivation – Problems

Problem 1

Evidence for **purely stringy constraints** that are **only seen** in **exact CFT** calculation on the **orbifold** and **NOT** on **CY**

[Blaszczyk, Groot Nibbelink, FR, Trapletti, Vaudrevange]

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Need a framework capable of **describing** both **departure** from the **orbifold** and **torsion**

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Suggestion

Use **Gauged Linear Sigma Models**

Outline

- 1 Gauged Linear Sigma Models
 - Definition
 - Anomalies
- 2 Example
- 3 Conclusion

Definition of GLSM

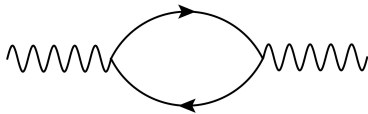
Consider **2D SUSY** with **Abelian** gauge groups and field content:

superfield type	notation	charge	bosonic DOF	fermionic DOF
chiral	Ψ^a	$(q_I)^a$	z^a	ψ^a
chiral-Fermi	Λ^α	$(Q_I)^\alpha$	h^α	λ^α
gauge	$(V, A)^I$	0	$a_{\sigma}^I, a_{\bar{\sigma}}^I$	Φ^I
Fermi-gauge	σ^i	0	s^i	φ^i
chiral	Φ^m	$(q_I)^m$	x^m	ψ^m
chiral-Fermi	Γ^μ	$(Q_I)^\mu$	–	γ^μ

Geometry given by **D-terms** and **F-terms**

Gauge group given by **monad bundle**

Anomalies



$$A_{IJ} := q_I \cdot q_J - Q_I \cdot Q_J,$$

$$q_I \cdot q_J := \sum_a (q_I)^a (q_J)^a + \sum_m (q_I)^m (q_J)^m,$$

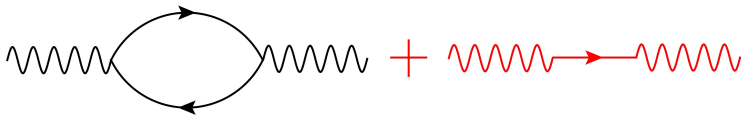
$$Q_I \cdot Q_J := \sum_\alpha (Q_I)^\alpha (Q_J)^\alpha + \sum_\mu (Q_I)^\mu (Q_J)^\mu.$$

Problem

In general **many** $U(1)$ gauge groups

\Rightarrow **Huge amount** of stringent **anomaly conditions**.

Anomalies



$$A_{IJ} := q_I \cdot q_J - Q_I \cdot Q_J + \mathcal{T}_{IJ},$$

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Idea

Introduce **new fields** to obtain **Green-Schwarz mechanism** on the world-sheet to **cancel gauge anomalies**. [Adams,Ernebjerg,Lapan]

Green–Schwarz mechanism

Green–Schwarz mechanism needs fields that transform with shifts.

Our approach

⇒ Use **logarithm** of **coordinate fields** Ψ

$$W_{\text{FI}} = \left[\rho_i^0 + T_{X_I} \ln |R^X(\Psi)| \right] F^I \quad \Rightarrow \quad \mathcal{T}_{IJ} = r_i^X T_{X_I}$$

$$A_{IJ} = q_I \cdot q_J - Q_I \cdot Q_J + \mathcal{T}_{IJ}$$

with

- ρ_i^0 : constant FI parameter
- $R^X(\Psi)$: homogeneous polynomials w/ charges r_i^X
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Consequences

$$H = dB + \omega_L - \omega_{YM}$$

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BIs on **CY** \leftrightarrow **Modular invariance** on **orbifold**.

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NS5 and anti-NS5 branes, torsion

- $\text{tr} \mathcal{R}^2 < \text{tr} \mathcal{F}^2 \Rightarrow$ **NS5** and **torsion**
- $\text{tr} \mathcal{R}^2 > \text{tr} \mathcal{F}^2 \Rightarrow$ **anti-NS5** and **torsion**
- $[\text{tr} \mathcal{R}^2] = [\text{tr} \mathcal{F}^2] \Rightarrow$ **torsion**

Example

1.) No anomalies

superfield	$\Psi^{a=1,\dots,8}$	$\Gamma^{\mu=1,\dots,4}$	$\Lambda^{\alpha=1,\dots,8}$	$\Phi^{m=1,\dots,4}$
lowest component	z^a	γ^μ	λ^α	x^m
gauge charge	1	-2	1	-2

$\mathbb{P}^7[2, 2, 2, 2]$ with $SU(3)$ bundle

$$\mathcal{A}_{11} = \frac{1}{2} [q_1^2 - Q_1^2 + \mathcal{T}_{11}]$$

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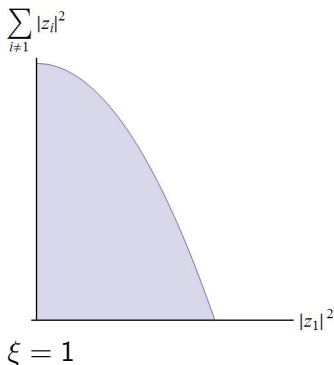
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$$\mathcal{T}_{11} = T = 0$$

1.) No anomalies



$$\xi > 0 \Rightarrow |x^a| = 0, \quad V_D \stackrel{!}{=} 0 \Rightarrow \sum_{a=1}^8 |z^a|^2 = \xi$$

Geometry **compact**, no anomalies.

2.) $T > 0$, compact geometry, effective curve

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$\mathbb{P}^7[2, 2, 2, 2]$ with $SU(2)$ bundle

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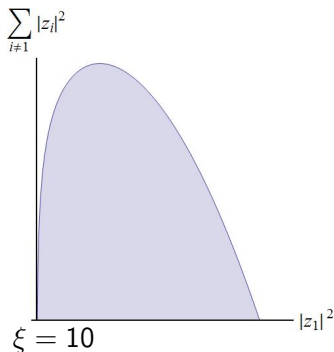
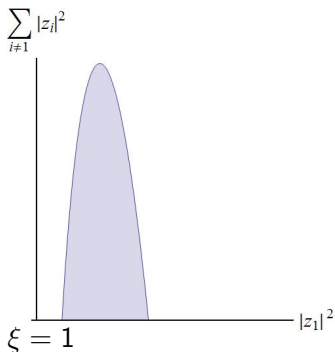
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Geometry still **compact**, anomalies canceled by **NS5 branes**.

3.) $T < 0$, decompactified geometry, non-effective curve

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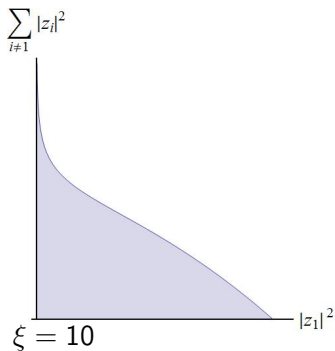
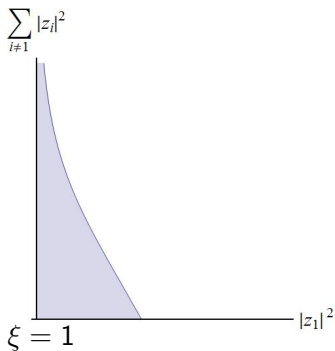
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Geometry **decompactified**, anomalies canceled with **anti-NS5 branes**.

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GLSMs powerful tool for string model building.

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Thank you for your attention!