

Abundance of Thermal WIMPs in Non-standard Cosmological Scenarios

Mitsuru Kakizaki (Bonn Univ.)

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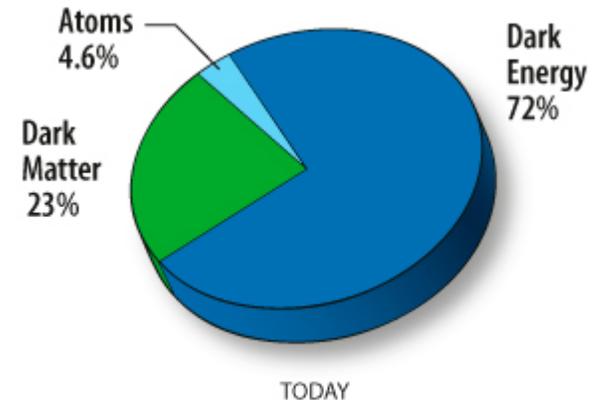
In collaboration with

- Manuel Drees (Bonn Univ.)
- Hoernisa Iminniyaz (Univ. of Xinjiang)

Refs:

- PRD73, 123502 (2006) [hep-ph/0603165]
- PRD76, 103524 (2007) [arXiv:0704.1590 [hep-ph]]

1. Motivation



[<http://map.gsfc.nasa.gov>]

- Observations of
 - cosmic microwave background
 - structure of the universe
 - etc.

➔ Non-baryonic cold dark matter: $\Omega_{\text{DM}} h^2 = 0.1099 \pm 0.0062$

- Weakly interacting massive particles (WIMPs) χ are good candidates for cold dark matter (CDM)

The predicted thermal relic abundance naturally explains the observed dark matter abundance: $\Omega_{\chi, \text{standard}} h^2 \sim 0.1$

- Neutralino (LSP); 1st KK mode of the B boson (LKP); etc.

Investigation of early universe using CDM abundance

- The relic abundance of thermal WIMPs is determined by the Boltzmann equation:

$$\dot{n}_\chi + 3Hn_\chi = -\langle\sigma_{\text{eff}}v\rangle(n_\chi^2 - n_{\chi,\text{eq}}^2)$$

(and the reheat temperature: T_R)

- The (effective) cross section σ_{eff} can be (hopefully) determined from collider and DM detection experiments

→ We can test the standard CDM scenario and investigate conditions of very early universe: T_R, H, \dots

- Standard scenario or non-standard scenarios?

[Scherrer; Salati; Rosati; Profumo, Ullio; Pallis; Maisero, Pietroni, Rosati; ...]

Outline

This work

- We provide an approximate analytic treatment that is applicable to low-reheat-temperature scenarios
- Based on the assumption that dark matter is made of thermal WIMPs,
 - we derive the lower bound on the reheat temperature
 - we constrain possible modifications of the Hubble parameter

c.f. Cosmic p^+, γ  Bounds on pre-BBN expansion

[Schelke, Catena, Fornengo, Masiero, Pietroni PRD74 (2006);
Donato, Fornengo, Schelke, JCAP0703 (2007)]

1. Motivation
2. Standard calculation of WIMP relic abundance
3. Low-temperature scenario
4. Constraints on the very early universe from WIMP dark matter
5. Summary

2. Standard calculation of the WIMP relic abundance

[Scherrer, Turner, PRD33(1986); Griest, Seckel, PRD43(1991); ...]

- Conventional assumptions:

- $\chi = \bar{\chi}$, single production of χ is forbidden
- Thermal equilibrium was maintained:

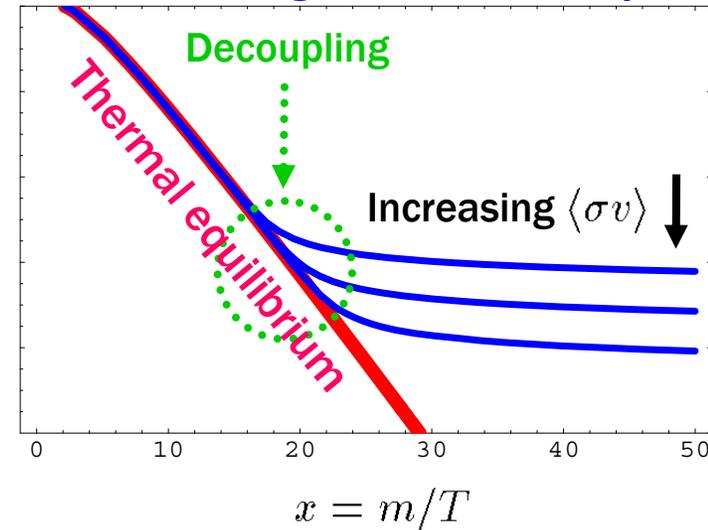
$$T_R(\text{Reheat temp}) \geq T_F(\text{Freezeout temp})$$

- For adiabatic expansion the Boltzmann eq. is

$$\frac{dY_\chi}{dx} = -\frac{\langle\sigma v\rangle s}{Hx} (Y_\chi^2 - Y_{\chi,\text{eq}}^2),$$

$$Y_{\chi(\text{,eq})} = \frac{n_{\chi(\text{,eq})}}{s}, \quad x = \frac{m_\chi}{T}$$

Co-moving number density



- χ decoupled when they were non-relativistic in RD epoch:

$$\langle\sigma v\rangle = a + 6b/x + \mathcal{O}(1/x^2), \quad n_{\chi,\text{eq}} = g_\chi (m_\chi T/2\pi)^{3/2} e^{-m_\chi/T}$$



$$\Omega_{\chi,\text{standard}} h^2 \simeq 0.1 \times \left(\frac{a + 3b/x_F}{10^{-9} \text{ GeV}^{-2}} \right)^{-1} \left(\frac{x_F}{22} \right) \left(\frac{g_*}{90} \right)^{-1/2} \sim \Omega_{\text{DM}} h^2$$

3. Low-temperature scenario

- Assumptions: $T_R \leq T_F$; $Y_\chi(x_0) = 0$, $x_0 = m_\chi/T_R$
- Zeroth order approximation: For $T_R \ll T_F$, χ annihilation is negligible:

$$\frac{dY_0}{dx} = 0.028 g_\chi^2 g_*^{-3/2} m_\chi M_{\text{Pl}} e^{-2x} x \left(a + \frac{6b}{x} \right)$$

The solution Y_0 is proportional to the cross section:

- First order approximation:

- Add a correction term describing annihilation to Y_0 : $Y_1 = Y_0 + \delta$ ($\delta < 0$)
- As long as $|\delta| \ll Y_0$, the evolution equation for δ is

$$\frac{d\delta}{dx} = -1.3 \sqrt{g_*} m_\chi M_{\text{Pl}} \left(a + \frac{6b}{x} \right) \frac{Y_0(x)^2}{x^2}$$

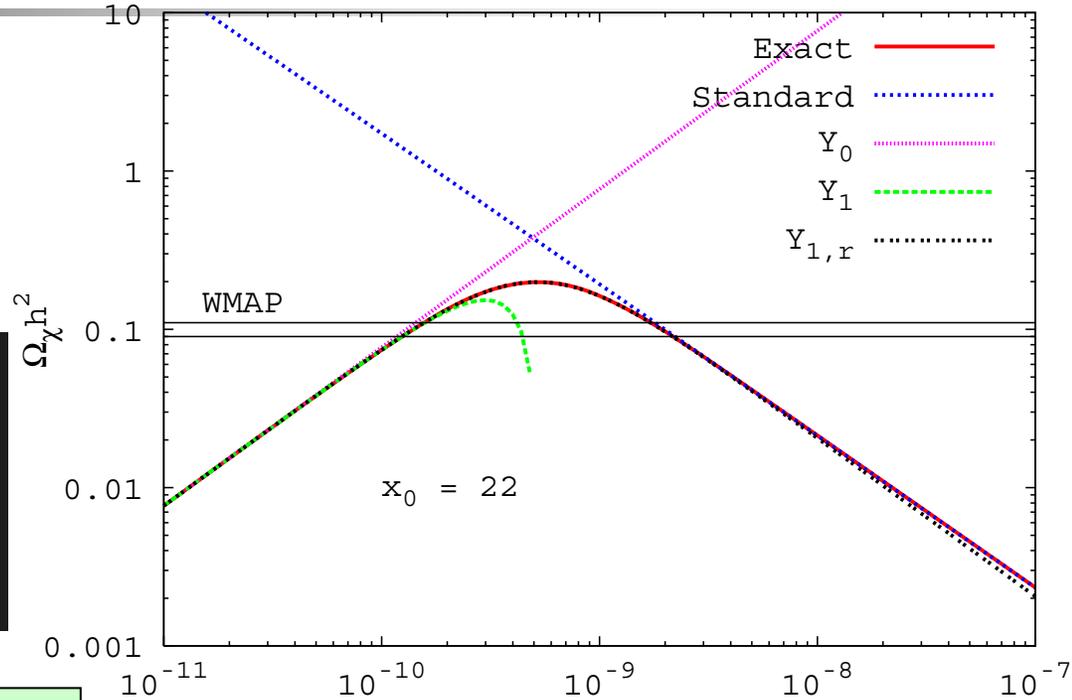
An analytic expression for δ can be obtained and is proportional to σ^3

Resummed ansatz

- We can obtain an excellent analytic formula for $T_R \leq T_F$ through resummation:

$$Y(x) = Y_0 + \delta = Y_0 \left(1 + \frac{\delta}{Y_0} \right)$$

$$\simeq \frac{Y_0}{1 - \delta/Y_0} \equiv Y_{1,r}$$



- For $|\delta| \gg Y_0$, $Y_{1,r}(x) \simeq -\frac{Y_0^2}{\delta} \propto \frac{1}{\sigma}$

$x_0 \rightarrow x_F \rightarrow$ **Standard formula**

x_0 (indicated by a green arrow pointing to the peak of the Standard curve)

At late times, $Y_{1,r}(x \rightarrow \infty) = \frac{1.3 \sqrt{g_*} m_\chi M_{\text{Pl}} (a + 3b/x_0)}{1.3 \sqrt{g_*} m_\chi M_{\text{Pl}} (a + 3b/x_0)}$

4. Constraints on the very early universe from WIMP DM

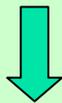
- Out-of-equilibrium case: $\sigma \nearrow \rightarrow \Omega h^2 \nearrow$; $T_R = m_\chi/x_R \nearrow \rightarrow \Omega h^2 \nearrow$
- Equilibrium case: $\sigma \nearrow \rightarrow \Omega h^2 \searrow$; $\Omega_\chi h^2$ is independent of T_R

• Thermal relic abundance:

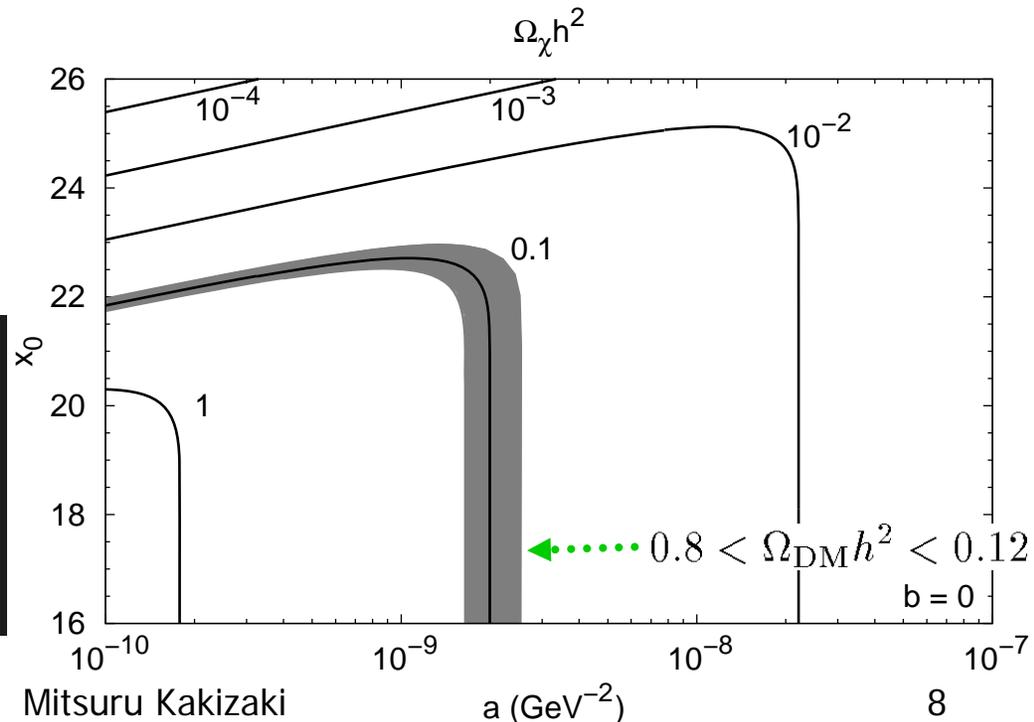
Assumption:

WIMPs are assumed to be produced in the RD epoch

Requirement that $\Omega_\chi h^2 \simeq 0.1$



Lower bound on the reheat temperature: $T_R > m_\chi/23$



Modified expansion rate

- Various cosmological models predict a non-standard early expansion

→ Predicted WIMP relic abundances are also changed

- Idea:

Once we know $\sigma, \Omega_{\text{DM}} h^2$

→ Constraint on the expansion rate at around WIMP decoupling
(within the framework of thermal WIMP production)

- Parametrization: $A(z) = H_{\text{st}}(z)/H(z)$, $z \equiv T/m_\chi = 1/x$
- We need to know $A(z)$ only for $z_{\text{BBN}} = 10^{-5} - 10^{-4} \leq z \leq z_F \sim 1/20 \ll \mathcal{O}(1)$

→ Taylor expansion of $A(z)$ in powers of $(z - z_{F,\text{st}})$:

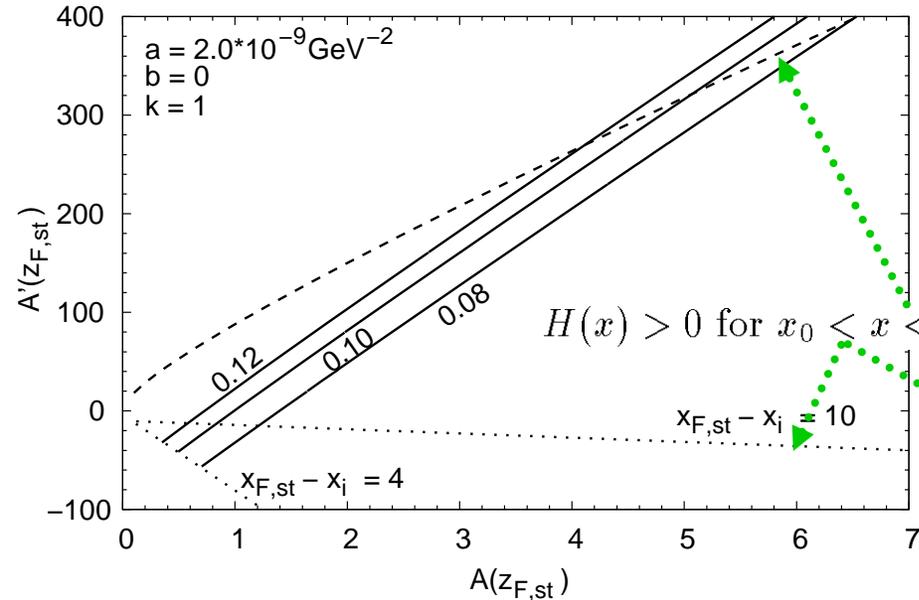
$$A(z) = A(z_{F,\text{st}}) + (z - z_{F,\text{st}})A'(z_{F,\text{st}}) + \frac{1}{2}(z - z_{F,\text{st}})^2 A''(z_{F,\text{st}})$$

Subject to the BBN limit: $k \equiv A(z \rightarrow z_{\text{BBN}}) \simeq 1$

Constraints on modifications of the Hubble parameter

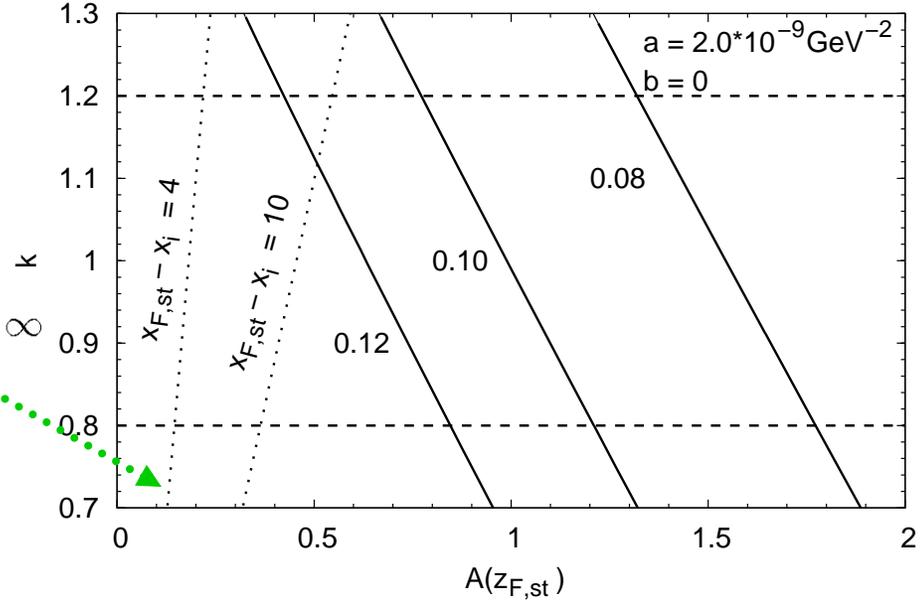
- Case for $k \equiv A(z \rightarrow z_{\text{BBN}}) = 1$

$$\Omega_\chi h^2$$



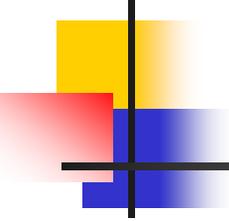
- Case for $A''(z_{F,st}) = 0$

$$\Omega_\chi h^2$$



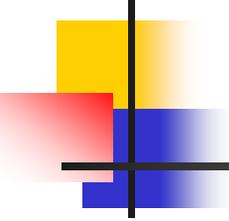
x_i : Maximal temperature below which our expansion is valid

$\Omega_\chi h^2$ depends on all $H(T_{\text{BBN}} < T < T_F)$ \Rightarrow Weaker constraints on $H(T_F)$



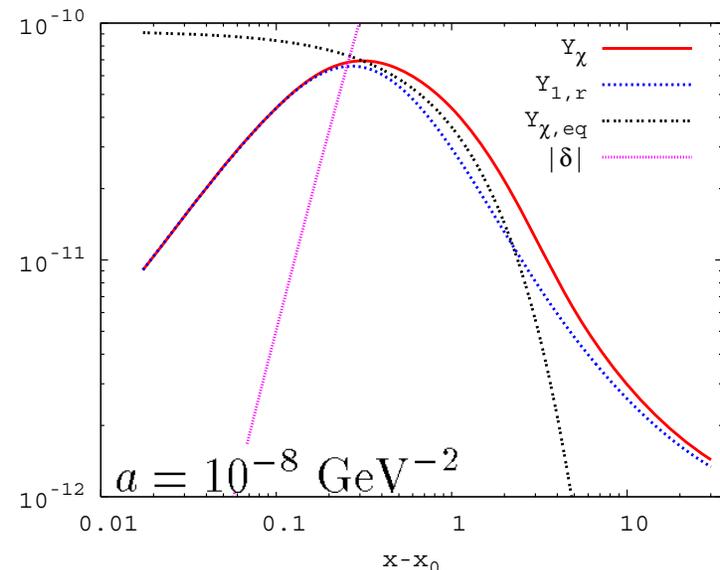
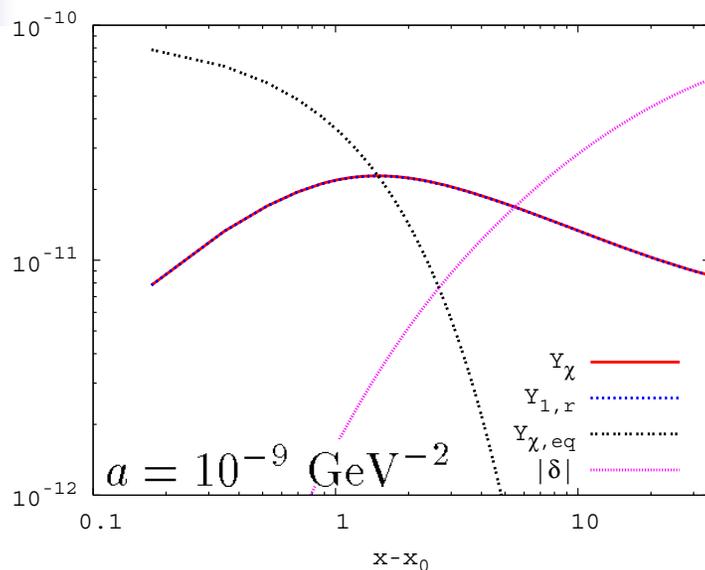
5. Summary

- Using the CDM relic density we can examine very early universe at around $T \sim m_\chi/20 \sim \mathcal{O}(10)$ GeV (well before BBN: $T_{\text{BBN}} \sim \mathcal{O}(1)$ MeV)
- We find an approximate analytic formula that is valid for all $T_R \leq T_F$
- By requiring $\Omega_{\chi,\text{thermal}} h^2 = \Omega_{\text{DM}} h^2$,
we found the lower bound on the reheat temperature: $T_R > m_\chi/23$
- The sensitivity of $\Omega_{\chi,\text{thermal}} h^2$ on $H(T_F)$ is weak
because $\Omega_{\chi,\text{thermal}} h^2$ depends on all $H(T_{\text{BBN}} < T < T_F)$



Backup slides

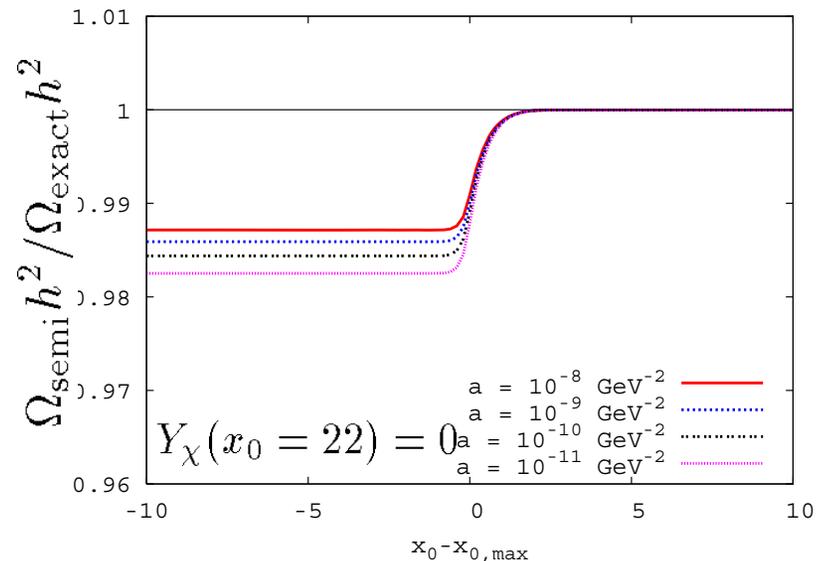
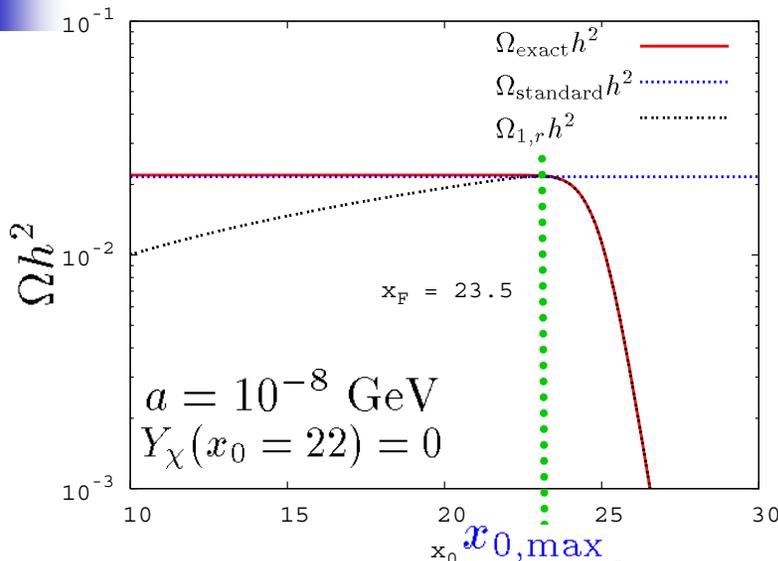
Evolution of solutions



Y_χ : Exact result, $Y_{1,r}$: Re-summed ansatz, $b = 0$, $Y_\chi(x_0 = 22) = 0$

- The re-summed ansatz $Y_{1,r}$ describes the full temperature dependence of the abundance when equilibrium is not reached
- For larger cross section the deviation becomes sizable for $x - x_0 \sim 1$, but the deviation becomes smaller for $x \gg x_0$

Semi-analytic solution



- $Y_{1,r}(x_0, x \rightarrow \infty) (\propto \Omega_{1,r} h^2)$ has a maximum (left)
- New semi-analytic solution can be constructed: $\Omega_{\text{semi}} h^2$ (right)

For $x_0 > x_{0,\text{max}}$, use $Y_{1,r}(x_0)$; for $x_0 < x_{0,\text{max}}$, use $Y_{1,r}(x_{0,\text{max}})$

The semi-analytic solution $\Omega_{\text{semi}} h^2$ reproduces the correct final relic density $\Omega_{\text{exact}} h^2$ to an accuracy of a few percent